



# A novel framework to intercept GPS-denied, bomb-carrying, non-military, kamikaze drones: Towards protecting critical infrastructures

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## ABSTRACT

Protection of urban critical infrastructures (CIs) from GPS-denied, bomb-carrying kamikaze drones (G-B-KDs) is very challenging. Previous approaches based on drone jamming, spoofing, communication interruption and hijacking cannot be applied in the case under examination, since G-B-KDs are uncontrolled. On the other hand, drone capturing schemes and electromagnetic pulse (EMP) weapons seem to be effective. However, again, existing approaches present various limitations, while most of them do not examine the case of G-B-KDs. This paper, focuses on the aforementioned under-researched field, where the G-B-KD is confronted by two defensive drones. The first neutralizes and captures the kamikaze drone, while the second captures the bomb. Both defensive drones are equipped with a net-gun and an innovative algorithm, which, among others, estimates the locations of interception, using a real-world trajectory model. Additionally, one of the defensive drones is also equipped with an EMP weapon to damage the electronics equipment of the kamikaze drone and reduce the capturing time and the overall risk. Extensive simulated experiments and comparisons to state-of-art methods, reveal the advantages and limitations of the proposed approach. More specifically, compared to state-of-art, the proposed approach improves: (a) time to neutralize the target by at least 6.89%, (b) maximum number of missions by at least 1.27% and (c) total cost by at least 5.15%.

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## 1. Introduction

A nation's productivity, quality of life and economic progression, heavily depend on CIs. Their importance is such that their inability or destruction could have a severe impact on national defense, economic stability, and public safety. For these reasons, CIs often become top-level targets. Well-known serious incidents include: (a) the UAV attack on Aramco's Abqaiq and Khurais facilities in August 2019, resulting in the disruption of 50% of the Kingdom of Saudi Arabia's primary asset, the world's largest oil production center. A swarm of 10 UAVs carried out this severe attack [1], (b) the January 2023 bomb-carrying UAVs' attack on an Iranian defense factory in the central city of Isfahan. The attack caused some damage at the plant [2], (c) the December 2018 flights disruption at Gatwick Airport, due to UAVs. The Airport suspended all flights to

avoid collision between UAVs and aircraft. The incident led to the diversion or cancellation of approximately 1000 flights, impacting around 140,000 passengers. The investigation incurred a cost of €800,000 [3].

In our previous research [4], neighboring CIs are considered, which are endangered by trucks, carrying explosive substances. Threat analysis covers three different scenarios and Voronoi tessellation is incorporated to limit the area of assessment. This paper significantly extends [4] by confronting aerial instead of ground threats. In particular it focuses on intercepting G-B-KDs, to protect urban CIs, where typically strict restrictions are applied on the use of anti-aircraft weapons, including missiles. G-B-KDs achieve self-navigation without GPS or remote control (using e.g. pre-installed satellite maps, cameras and artificial intelligence). It is also assumed that they are rigged with explosives and carry a releasable bomb, while their mission is to cause maximum damage to the target CI.

In the literature, several works have focused on civilian drones' stopping strategies, based on jamming, spoofing, communication interruption or hijacking [5]. However, these schemes cannot be

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applied in the case under examination, since G-B-KDs are uncontrolled. On the other hand, drone capturing schemes and EMP weapons can be effective. However, existing approaches either examine net/catching technologies or EMP to neutralize drones, without combining both. Furthermore, locations of interception are estimated in few approaches. Additionally, most schemes do not consider drones carrying bombs.

The proposed scheme is classified among drone capturing approaches, incorporating EMP, a net gun and a novel interception algorithm. In particular, two defensive drones (DDs) confront the G-B-KD. The first DD neutralizes and captures the G-B-KD, while the second DD captures the bomb. To succeed to their missions: (a) both DDs are equipped with a net-gun and run an innovative algorithm, which, among other, estimates the most likely trajectory locations to intercept and capture the bomb and the G-B-KD and (b) the first DD is also equipped with an EMP weapon to damage the electronics of the G-B-KD.

To summarize, the major contributions of this paper are:

- It examines the under-researched field of kamikaze drones carrying releasable bombs of different Relative Effectiveness Factors in urban environments, which has not been comprehensively studied in the literature.
- It investigates DDs equipped both with net-guns and EMP, in contrast to existing methods, which propose either a net/catching technology or EMP.
- It establishes a real-world model of the trajectory of the bomb and G-B-KD in case of free fall with air resistance.
- It proposes a novel algorithm, which, among others, estimates the locations of interception, using the real-world trajectory model.
- It provides simulated experiments, using real world parameters, while it carries out extensive comparisons to state-of-art methods.

The remainder is organized as follows: Section 2 presents background information. Section 3 explores related work. Section 4 outlines the proposed scheme, with simulated results and comparisons presented in Section 5. Lastly, Section 6 concludes the paper, highlighting potential future research.

## 2. Background

### 2.1. Definitions and background information

- Atmospheric pressure at sea level: 1 atm (=14.696 psi).
- Gauge pressure: pressure variance between a supply tank and the surrounding air (disregarding atmospheric pressure).
- Overpressure: pressure resulting from a shock wave exceeding the standard atmospheric pressure.
- Relative Effectiveness Factor (REF): provides a comparison of a substance's explosive capability to the respective explosive capability of Trinitrotoluene.

Table 1 [6] outlines the anticipated infrastructure damage based on overpressure. As observed, overpressures >1 may cause serious damage.

### 2.2. REF of various substances

Let  $S_i$ ,  $i = 1, 2, \dots, n$ , be an explosive substance. Let also  $REF(S_i^U)$  express the REF per unit for each different  $S_i$ . Table 2 [7–10] provides the REF for various  $S_i$ 's.

For example, if 1 kg of Trinitrotoluene demolishes a wall, then 0.42 kg (1.0/2.38) of octanitrocubane can achieve the same result.

### 2.3. Blast-waves

When an  $S_i$  explodes it produces a shock wave, which is depicted in Fig. 1 [11] (pressure-time waveform). The ideal waveform is visualized for a distance  $r_c$  from the center of the blast. The atmospheric pressure is denoted by  $P_{atm}$ , while the positive phase, the negative phase and the time of arrival are denoted by  $t_{pos}$ ,  $t_{neg}$  and  $t_{ar}$  respectively. Additionally,  $pim_o$  denotes the positive incident impulse,  $P_{ov}$  denotes the peak overpressure and  $P_{un}$  denotes the peak underpressure. Then [11]

$$P(t) = P_{atm} + P_{ov} \frac{(t_{pos} - t)}{t_{pos}}, 0 < t \leq t_{pos} \quad (1)$$

and more accurately [11]

$$P(t) = P_{atm} + P_{ov} e^{-\delta t} \quad (2)$$

where the decay rate is denoted by  $\delta$ , while  $t_{ar}$  is used to start measuring  $t$ .

Moreover,  $PR_f$  that denotes the proximity factor can be calculated by [12,13].

$$PR_f = \frac{r_c}{\sqrt[3]{M_e}} \quad (3)$$

where  $M_e$  denotes the mass of the explosive in kilograms (Trinitrotoluene). Blast-waves have been extensively studied and this paper adopts the formula of Ref. [14], which covers all distances

$$P_{ov} = P_{atm} \frac{808 \left[ 1 + \left( \frac{PR_f}{4.5} \right)^2 \right]}{\sqrt{\left[ 1 + \left( \frac{PR_f}{0.048} \right)^2 \right]} \cdot \sqrt{\left[ 1 + \left( \frac{PR_f}{0.32} \right)^2 \right]} \cdot \sqrt{\left[ 1 + \left( \frac{PR_f}{1.35} \right)^2 \right]}} \quad (4)$$

And by expressing Eq. (4) using distance and mass

$$P_{ov} = P_{atm} \frac{808 \left[ 1 + \left( \frac{r_c}{4.5 \sqrt[3]{M_e}} \right)^2 \right]}{\sqrt{\left[ 1 + \left( \frac{r_c}{0.048 \sqrt[3]{M_e}} \right)^2 \right]} \cdot \sqrt{\left[ 1 + \left( \frac{r_c}{0.32 \sqrt[3]{M_e}} \right)^2 \right]} \cdot \sqrt{\left[ 1 + \left( \frac{r_c}{1.35 \sqrt[3]{M_e}} \right)^2 \right]}} \quad (5)$$

**Table 1**  
Damage to CI versus overpressure.

Overpressure	Possible damage
$0.4 \times 10^{-1}$	Booming sound that may damage glasses
$1.5 \times 10^{-1}$	Destruction of glasses
$4 \times 10^{-1}$	Modest damage on the structure of a building
$5 \times 10^{-1} - 10 \times 10^{-1}$	Destruction of windows as well as window-frames
$7 \times 10^{-1}$	Modest destruction to the structure of homes
$10 \times 10^{-1}$	Partial destruction of homes
$10 \times 10^{-1} - 20 \times 10^{-1}$	Collapse and warping of corrugated metal panels & Blow away of residential panels made of wood
$10 \times 10^{-1} - 80 \times 10^{-1}$	Injuries, varying from minor to severe lacerations caused by airborne glass and other projectiles
$20 \times 10^{-1}$	Partial failure of residential walls and roofs
$20 \times 10^{-1} - 30 \times 10^{-1}$	Destruction of walls made by cement that is not reinforced or by concrete blocks
$24 \times 10^{-1} - 122 \times 10^{-1}$	Tympanic membrane perforation for 1 to 90 percent among humans
$25 \times 10^{-1}$	House brick construction is destroyed by 50 percent
$30 \times 10^{-1}$	Steel-framed structures warped and detached from their foundation
$50 \times 10^{-1}$	Destruction of Electricity Power Poles
$50 \times 10^{-1} - 70 \times 10^{-1}$	Homes are almost completely destroyed
$70 \times 10^{-1}$	Railroad cars are tipped over
$90 \times 10^{-1}$	Cargo train box cars are destroyed
$100 \times 10^{-1}$	Buildings are totally destroyed
$145 \times 10^{-1} - 290 \times 10^{-1}$	Human casualties in the range of 1–99 percent, resulting from immediate blast impact

**Table 2**  
 $REF(S_i^d)$  for various  $S_i$ 's.

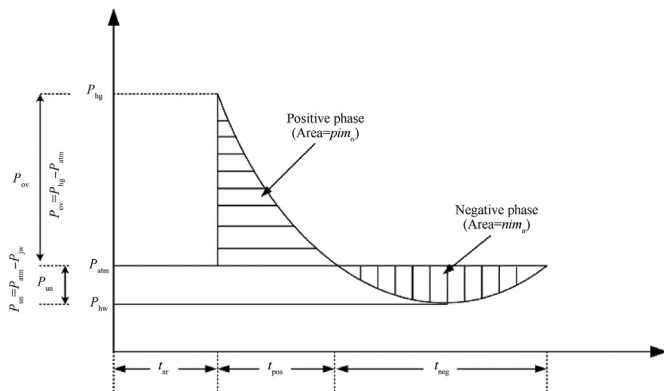
Chemical formula of $S_i$	$REF(S_i^d)$
$C_7H_5N_3O_6$ (Trinitrotoluene)	$10 \times 10^{-1}$
$NH_4NO_3$	$3.2 \times 10^{-1}$
$C_6H_{12}N_4O_8$	$6 \times 10^{-1}$
$C_6H_4(NO_2)_2$	$6 \times 10^{-1}$
$NH_4NO_3 + C_nH_{2n+2}$ (ANFO)	$7.4 \times 10^{-1}$
$CH_4N_2O_3$	$10.5 \times 10^{-1}$
$(C_6H_7O_2(ONO_2)_3)_n$	$11 \times 10^{-1}$
$C_6H_3N_3O_7$	$11.7 \times 10^{-1}$
$C_6H_3N_3O_6$	$12 \times 10^{-1}$
$C_3H_5N_3O_9$ (Nitroglycerin)	$15.4 \times 10^{-1}$
$C_3H_6N_6O_6$	$16 \times 10^{-1}$
$C_8(NO_2)_8$ (Octanitrocubane)	$23.8 \times 10^{-1}$

**Table 4**  
Classification of drones according to range/endurance.

Drone Range Category	Range/km	Endurance/h
Very Close	<5	0.5–0.75
Close	>5 & <50	1–6
Short	>50 & <150	8–12
Medium	>150 & <650	12–48
Long	>650	>48

**Table 5**  
Characteristic non-military UAVs [18–27].

Name	Max Payload/kg	Max Speed/(km · h <sup>-1</sup> )	Price/Euro
Griff 800	800	50	240,000
SF-DL-180	100	100	36,000
MH-50	50	36	12,000
JT16L-404QC	22	43	4200
Goliath Quadcopter	18	130	1300
OnyxStar Hydra-12	16	35	4000
YangDa Skywhale Max	15	130	32,000
Freefly Alta X	10	95	17,000
DJI Matrice 300 RTK	2.7	83	13,800
DRL Racer X	1	289	NA



**Fig. 1.** Wave form of a blast in the open air.

2.4. Non-military UAVs

Various factors can be used to categorize drones. The most

common include weight, type of engine, maximum value of flying altitude, autonomy capabilities, role and more. The United States Department of Defense (USDOD), divides drones into five distinct categories [15] (Table 3). Drones can also be classified according to range and endurance (Table 4).

Regarding the degree of autonomy, drones may be human-operated, or have different levels of autonomy, from automated piloting assistance to full autonomy [16,17].

Additionally, Table 5 provides some characteristic non-military drones, available on the market.

As it can be observed and as of January 2024, their maximum payload is between 1 kg and 800 kg, their maximum speed is

**Table 3**  
Classification of drones according to USDOD.

Group	G1	G2	G3	G4	G5
Max take-off weight	<9.1 kg	>9.1 kg & <25 kg	>25 kg & <600 kg	>600 kg	>600 kg
Operating altitude	<370 m	<1.1 km	<5.5 km	<5.5 km	>5.5 km
Speed	<190 km · h <sup>-1</sup>	<460 km · h <sup>-1</sup>	<460 km · h <sup>-1</sup>	Any	Any

between 35 km/h and 289 km/h and their price is between 1300 Euro and 240,000 Euro.

This paper focuses on relatively low-cost non-military drones, since terrorists can easily find them and turn them into G-B-KDs. It should also be mentioned that military drones need completely different weapons to be neutralized (e.g. MANPADS, surface-to-air missiles etc.)

### 3. Related work

One of the most serious threats that CIs face comes from terrorist drones [28,29]. In the past, several schemes have been proposed to confront this threat. In Ref. [30] multiple agents track and disable a rogue UAV by cooperatively transmitting power from their on-board antennas to jam its communication and sensing receivers. In Ref. [31] the pursuer agent integrates software-defined radio technology to execute rogue drone GPS disruption, while concurrently, autonomous agents collaborate to calculate the location estimate of the pursuer agent. Ref. [32] introduces a narrow beam directors-based Vivaldi antenna, which is designed to cover remotely piloted aircraft system bands. The antenna works as portable anti-drone jammer. In Ref. [33] a Software Defined Radio board is integrated to deploy an RF-based technique for detecting, identifying, and jamming drones. The suggested approach disrupts the wireless link between the drone and ground over the widely utilized frequency of 2.4 GHz. In Ref. [34] a mechanism for detecting drones is suggested. The method utilizes the RF control signal that the drone receives from the remote controller. Subsequently, a high-power signal jams the communication and severs the connection with the controller. In Ref. [35] multiple surveillance drones patrol an area. They identify hostile drones using image processing, surround them and initialize cyber-attacks. In Ref. [36] the DronEnd system incorporates scanning of the RF spectrum, detection of hostile drones based on Angle of Arrival algorithms, and annihilation by RF jamming. Ref. [37] presents a portable system that incorporates software defined radio platforms. The scheme jams malicious drones by generating GPS spoofing signals.

Additionally, there are some neutralization schemes based on directed-energy weapons. In Ref. [38] a Helical Array Antenna releases EMP against commercial drones. Its strength for small ranges is tested, by examining the extent of damage to the drone's

electronics. Ref. [39] focuses on laser weapons against drones. The main factors are determined, such as power supply for laser and cooling equipment and system mass. In Ref. [40] machine learning facilitates decision support for warfighters, operating laser weapon systems in intricate tactical scenarios. Wargaming scenarios are simulated and the algorithm forecasts the optimal engagement strategy.

On the other hand, various systems and methods have been proposed to catch or neutralize drones. Ref. [41] presents a drone neutralization system centered around another drone, equipped with a capturing device. The operation depends solely on data recorded by a long-range and a short-range camera. In Ref. [42] a soft-gripper drone is proposed. To avoid aerodynamic disturbances, the gripper utilizes soft actuators, to maintain horizontal orientation and bend when subjected to air pressure. Ref. [43] augments the automation of physical interception operations and optimizes the efficiency of trajectories towards approaching the intruder-drone. Ref. [44] performs autonomous capture of drones, which navigate at various trajectories and speeds. The system also bursts many balloons, distributed randomly across a designated area. Ref. [45] neutralizes drones in GPS-denied. The platform employs a pre-trained model to detect, track, and pursue drones. Ref. [46] examines kinetic energy non-lethal weapons (KENLW) to neutralize low, small and slow drones. KENLWs launch fast-moving small projectiles. Ref. [47] implements a drone capture device, which uses protective covering to avoid dispersion of the capture net. Following the capture of the target, a pull-off force test is conducted to verify the net's stability. In Ref. [48] neutralization of drones is performed by a swarm of drones that carries a net. Optimal intersection is estimated and flight parameters are described. In Ref. [49] a soft-gripper robot has 3 fingers and touch sensors to accomplish safe capturing of drones. In Ref. [50] a team of drones carries a capture net, which is tensioned by properly adjusting the acceleration of each team-member. In Ref. [51] autonomous interception is achieved by a visual-based servo algorithm. In Ref. [52] a vision-based navigation method seeks and detects intruding drones. Then, the target trajectory is predicted by fusing onboard vision and inertial-measurement resources. Other interesting schemes and related surveys include Refs. [53–60].

Even though very interesting, most of the aforementioned schemes do not consider G-B-KDs. Additionally, they examine

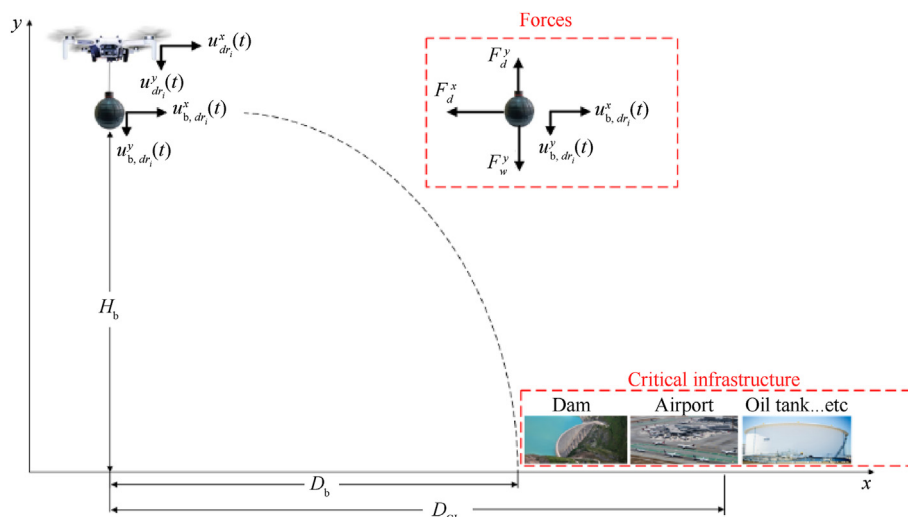


Fig. 2. Illustration of a G-B-KD approaching a CI.

either a net/catching technology or EMP, not both. Furthermore, few approaches estimate the location of interception, while existing algorithms cannot be applied in case of autonomous drones. The proposed scheme considers all these aspects, while its strengths and limitations are revealed through extensive experimentation on simulated data and comparison to the state-of-art.

#### 4. Problem formulation and the proposed scheme

##### 4.1. Problem formulation

In Fig. 2, a G-B-KD approaches a CI (dam, airport, oil tank, etc.). Without loss of generality, the G-B-KD and the bomb are moving on the  $xy$ -plane. In order to achieve maximum damage, the G-B-KD should: (a) release its bomb at a specific distance from the CI and (b) crash at the CI.

In order to find the horizontal distance  $D_b$  that a bomb will travel when released from a G-B-KD, let us denote by  $dr_i, i = 1, 2, \dots, n$ , the  $i$ -th G-B-KD that carries a bomb and tries to attack a CI. Let us also denote by: (a)  $u_{dr_i}^x(t)/u_{dr_i}^y(t)$  the horizontal/vertical velocity of the  $i$ -th G-B-KD and (b)  $u_{b,dr_i}^x(t)/u_{b,dr_i}^y(t)$  the horizontal/vertical velocity of the bomb of the  $i$ -th G-B-KD. Additionally, let us assume that the bomb is released at  $t = 0$  and at height  $H_b$ .  $D_{CI}$  is the horizontal distance of the bomb from CI. If  $D_b < D_{CI}$ , then the CI is not directly hit. However, its safety also depends on the blast pressure (Eq. (5) and Table 1).

$$\frac{d(ur_{b,dr_i}^y)}{dt} = g \left( 1 - \frac{(ur_{b,dr_i}^y)^2}{(ur_{term}^y)^2} \right) = > \frac{d(ur_{b,dr_i}^y)}{\left( 1 - \frac{(ur_{b,dr_i}^y)^2}{(ur_{term}^y)^2} \right)} = g dt = > \int \frac{d(ur_{b,dr_i}^y)}{\left( 1 - \frac{(ur_{b,dr_i}^y)^2}{(ur_{term}^y)^2} \right)} = g \int dt \quad (12)$$

In order to establish a real-world model of the trajectory of the bomb, the drag is taken into account. According to Ref. [61] up to velocities of about 877 km/h (800 ft/s) the simple square drag law holds for solid shell-like bodies.

Fig. 2 illustrates the forces exerted on the released bomb.  $F_d^x/F_d^y$  is the air resistance at the  $x/y$  axis, respectively, while  $F_w^y$  is the gravitational force. When the bomb is released from the G-B-KD, its trajectory will vary in curvature. Then, two-dimensional motion can be approximated by two one-dimensional motions, along the  $x$  and  $y$ -axis, since no analytic solution is possible for two-dimensional motions [62]. Additionally, the bomb is considered having a sphere's shape.

Initially the vertical motion is considered. In this case,  $F_d^y$  can be expressed by [62]

$$F_d^y = \frac{1}{2} \rho_a C_d A_b (ur_{b,dr_i}^y)^2 \quad (6)$$

where  $\rho_a$  is the density of the air,  $C_d$  is the drag coefficient,  $A_b$  is the effective cross-sectional area of the bomb and  $ur_{b,dr_i}^y$  is the relative velocity between the bomb and the air.

Then in the  $y$  direction we have

$$F_b^y = F_w^y - F_d^y \quad (7)$$

where the total force  $F_b^y$  can be expressed as

$$F_b^y = m_b \gamma_b^y \quad (8)$$

$m_b$  is the mass and  $\gamma_b^y$  is the acceleration of the bomb.

Additionally

$$F_w^y = m_b g \quad (9)$$

where  $g$  is the gravity.

Furthermore, when  $F_w^y = F_d^y$  then the bomb reaches terminal velocity ( $ur_{term}^y$ ). In this case

$$m_b g = \frac{1}{2} \rho_a C_d A_b (ur_{term}^y)^2 = > ur_{term}^y = \sqrt{\frac{2m_b g}{\rho_a C_d A_b}} \quad (10)$$

Then Eq. (7) becomes

$$m_b \gamma_b^y = m_b g - \frac{1}{2} \rho_a C_d A_b (ur_{b,dr_i}^y)^2 = > \gamma_b^y = g \left( 1 - \frac{(ur_{b,dr_i}^y)^2}{(ur_{term}^y)^2} \right) \quad (11)$$

To get the velocity-time formula, acceleration is integrated

By substituting

$$\frac{ur_{b,dr_i}^y}{ur_{term}^y} = w = > dw = \frac{d(ur_{b,dr_i}^y)}{ur_{term}^y} \quad (13)$$

$$ur_{term}^y \int \frac{\frac{d(ur_{b,dr_i}^y)}{ur_{term}^y}}{\left( 1 - \frac{(ur_{b,dr_i}^y)^2}{(ur_{term}^y)^2} \right)} = g \int dt = > ur_{term}^y \int \frac{dw}{1 - w^2} = g \int dt \quad (14)$$

Since

$$\int \frac{dw}{1 - w^2} = \operatorname{arctanh}(w) \quad (15)$$

Eq. (14) becomes

$$\operatorname{arctanh} \frac{ur_{b,dr_i}^y}{ur_{term}^y} = \frac{gt}{ur_{term}^y} + C \quad (16)$$

Since

$$\arctanh(y) = x \Rightarrow \tanh(x) = y \quad (17)$$

Eq. (16) becomes

$$ur_{b,dr_i}^y(t) = ur_{term}^y \tanh\left(\frac{gt}{ur_{term}^y} + C\right) \quad (18)$$

In our problem

$$ur_{b,dr_i}^y(0) = 0 \Rightarrow C = 0 \quad (19)$$

As a result, Eq. (18) becomes

$$ur_{b,dr_i}^y(t) = ur_{term}^y \tanh\left(\frac{gt}{ur_{term}^y}\right) \quad (20)$$

In order to calculate the position of the bomb at the y-axis as a function of time

$$y(t) = \int d(ur_{b,dr_i}^y) = ur_{term}^y \int \tanh\left(\frac{gt}{ur_{term}^y}\right) dt \quad (21)$$

And by making the following substitution

---


$$\gamma_b^x = \frac{d(ur_{b,dr_i}^x)}{dt} = -\frac{\rho_a C_d A_b}{2m_b} (ur_{b,dr_i}^x)^2 \Rightarrow \frac{d(ur_{b,dr_i}^x)}{(ur_{b,dr_i}^x)^2} = -\frac{\rho_a C_d A_b}{2m_b} dt \Rightarrow \int \frac{1}{(ur_{b,dr_i}^x)^2} d(ur_{b,dr_i}^x) = -\frac{\rho_a C_d A_b}{2m_b} \int dt \Rightarrow -\frac{1}{ur_{b,dr_i}^x} = -\frac{\rho_a C_d A_b}{2m_b} t + C \quad (32)$$

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$$\frac{gt}{ur_{term}^y} = z \Rightarrow \frac{ur_{term}^y}{g} dz = dt \quad (22)$$

Eq. (21) becomes

$$ur_{term}^y \int \tanh(z) \frac{ur_{term}^y}{g} dz = \frac{(ur_{term}^y)^2}{g} \int \tanh(z) dz \quad (23)$$

And since

$$\int \tanh(z) dz = \ln(\cosh(z)) + C \quad (24)$$

Eq. (23) becomes

$$y(t) = \frac{(ur_{term}^y)^2}{g} \ln\left(\cosh\left(\frac{gt}{ur_{term}^y}\right)\right) + C \quad (25)$$

In our problem:

$$y(0) = 0 \Rightarrow C = 0 \quad (26)$$

As a result, Eq. (25) becomes

$$y(t) = \frac{(ur_{term}^y)^2}{g} \ln\left(\cosh\left(\frac{gt}{ur_{term}^y}\right)\right) \quad (27)$$

Let us now consider the horizontal motion of the bomb

$$F_d^x = \frac{1}{2} \rho_a C_d A_b (ur_{b,dr_i}^x)^2 \quad (28)$$

where  $ur_{b,dr_i}^x$  is the relative velocity between the bomb and the air.

Then, in the x direction

$$F_b^x = -F_d^x \quad (29)$$

In this case

$$m_b \gamma_b^x = -\frac{1}{2} \rho_a C_d A_b (ur_{b,dr_i}^x)^2 \quad (30)$$

or

$$\gamma_b^x = -\frac{\rho_a C_d A_b}{2m_b} (ur_{b,dr_i}^x)^2 \quad (31)$$

To get the velocity-time formula, acceleration is integrated

where C is a constant. Since  $ur_{b,dr_i}^x(0) = u_{dr_i}^x(0)$ , from Eq. (32) we have

$$C = -\frac{1}{u_{dr_i}^x(0)} \quad (33)$$

Then Eq. (32) becomes

$$\frac{1}{ur_{b,dr_i}^x} = \frac{\rho_a C_d A_b}{2m_b} t + \frac{1}{u_{dr_i}^x(0)} \Rightarrow \frac{1}{ur_{b,dr_i}^x} = \frac{1}{u_{dr_i}^x(0)} \left(1 + \frac{\rho_a C_d A_b u_{dr_i}^x(0)}{2m_b} t\right) \quad (34)$$

And by denoting

$$\tau = \frac{2m_b}{\rho_a C_d A_b u_{dr_i}^x(0)} \quad (35)$$

Eq. (34) becomes

$$\frac{1}{ur_{b,dr_i}^x} = \frac{1}{u_{dr_i}^x(0)} \left(1 + \frac{t}{\tau}\right) \Rightarrow ur_{b,dr_i}^x(t) = \frac{u_{dr_i}^x(0)}{1 + \frac{t}{\tau}} \quad (36)$$

Then, the position of the bomb as a function of time is calculated



$$\frac{dx}{dt} = u_{b, dr_i}^x(t) = \frac{u_{dr_i}^x(0)}{1 + \frac{t}{\tau}} \Rightarrow dx = \frac{u_{dr_i}^x(0)}{1 + \frac{t}{\tau}} dt \Rightarrow \int dx$$

$$= \int \frac{u_{dr_i}^x(0)}{1 + \frac{t}{\tau}} dt \tag{37}$$

And since

$$\int \frac{1}{1+ax} dx = \frac{1}{a} \ln(1+ax) + C \tag{38}$$

Eq. (37) becomes

$$x(t) = u_{dr_i}^x(0)\tau \ln\left(1 + \frac{t}{\tau}\right) + C \tag{39}$$

In our problem

$$x(0) = 0 \Rightarrow C = 0 \tag{40}$$

As a result, Eq. (39) becomes

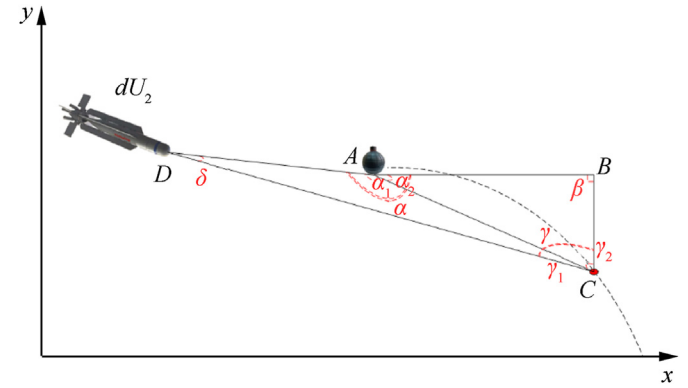


Fig. 4.  $dU_2$  moving towards the location of interception C (engagement with bomb).

$$x(t) = u_{dr_i}^x(0)\tau \ln\left(1 + \frac{t}{\tau}\right) \tag{41}$$

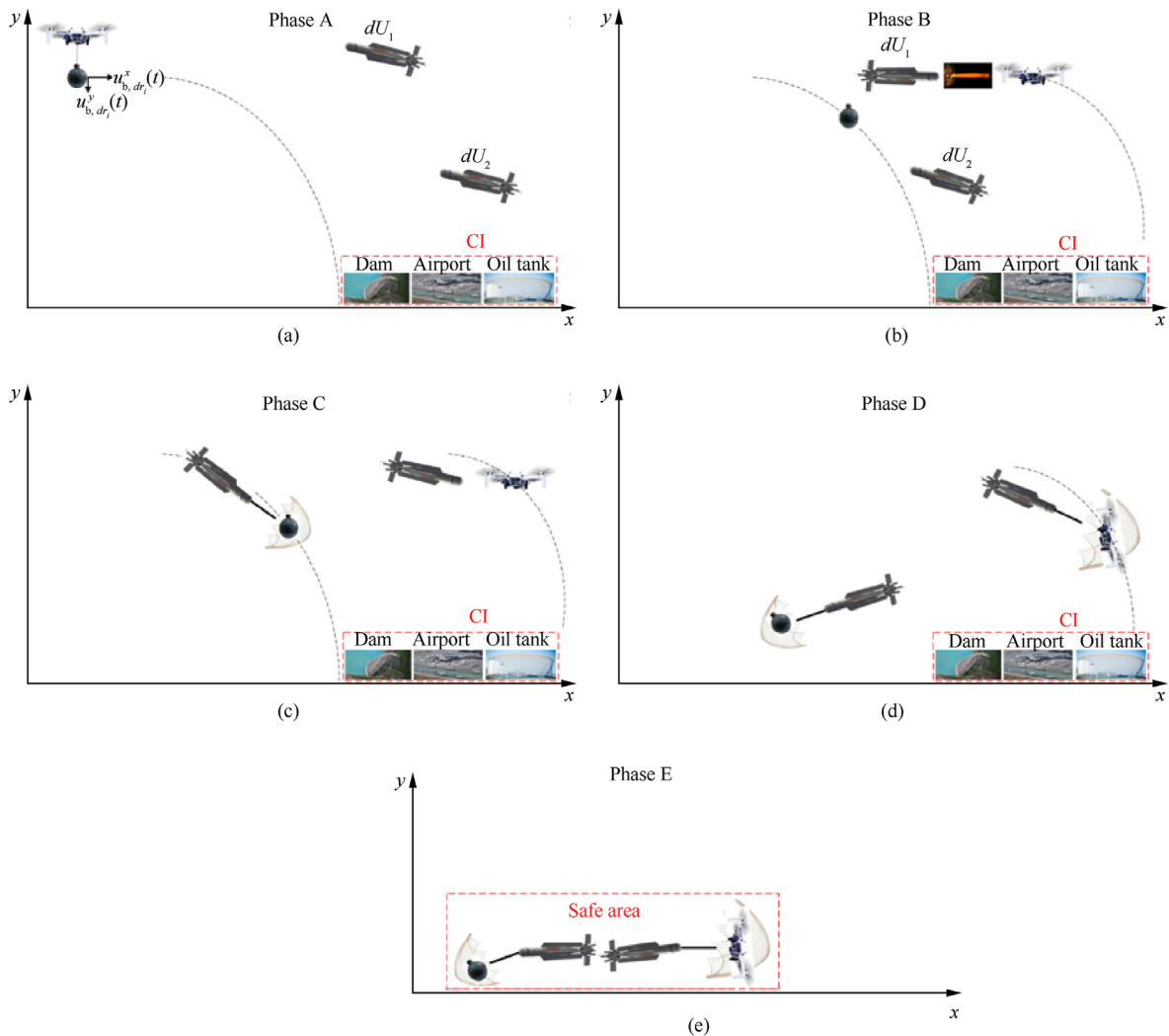


Fig. 3. (a) G-B-KD releasing a bomb.  $dU_1$  and  $dU_2$  on their way to intercept the threats; (b)  $dU_1$  releasing EMP.  $dU_2$  moving towards the location of interception with the bomb; (c)  $dU_2$  releasing the net and capturing the bomb.  $dU_1$  moving towards the location of interception with the G-B-KD; (d)  $dU_1$  releasing the net and capturing the G-B-KD.  $dU_2$  moving towards the safe area; (e)  $dU_1$  and  $dU_2$  at the safe area.

#### 4.2. The proposed scheme based on a couple of DDs

Let us assume that the G-B-KD is able to detect the DDs (e.g. by proximity sensors) and, in this case, it is programmed to release the bomb before the DDs arrive. Let us denote by  $dU_1$  and  $dU_2$  the two specially equipped DDs, where  $dU_1$  neutralizes and captures the G-B-KD, while  $dU_2$  captures the bomb.  $dU_1$  and  $dU_2$  are equipped with a net-gun and a processing unit which runs the proposed Algorithm 1, while  $dU_1$  is also equipped with an EMP weapon. Here, the following should be mentioned: (a) there are drones such as Raytheon Coyote Block 3 [63], which use EMP and drones that use net-guns [43,47,48,50] (b) to the best of the authors' knowledge there are not any drones that incorporate both weapons and utilize trajectory estimation (Eqs. (27) and (41)), so that to calculate the optimal locations of interception.

Additionally, let us assume that the maximum speeds that  $dU_1$  and  $dU_2$  can reach are  $u_{\max,dU_1}$  and  $u_{\max,dU_2}$  respectively. Then, the following conditions are required

$$u_{\max,dU_1} \gg u_{dr_i}^y(t) \ \& \ u_{\max,dU_1} \gg u_{dr_i}^x(t), \ \forall t \quad (42)$$

$$u_{\max,dU_2} \gg ur_{\text{term}}^y \quad (43)$$

According to Eq. (42),  $dU_1$  moves much faster than  $dr_i$ ,  $i = 1, 2, \dots, n$ , and according to Eq. (43),  $dU_2$  can reach speeds that highly surpass the terminal velocity of the bomb. Both conditions can be satisfied by different drones (e.g. Raytheon Coyote Block 2, reaches 555 km/h [64]).

Fig. 3 illustrates the five phases of the proposed framework, which may not necessarily be sequential. Additionally, phases are not in chronological order, e.g., Phase C may be completed before Phase B etc.

The locations of interception (with the bomb/G-B-KD) are the spatial points where  $dU_1$  intercepts the free-fall G-B-KD, (after Phase B) and  $dU_2$  intercepts the bomb. These locations can be estimated for all arrangements of G-B-KD, DDs and the bomb. An example is provided in Fig. 4. In particular, let us suppose that the interception location of  $dU_2$  and the bomb is C, where C is reached by both the bomb and  $dU_2$  at  $t = t_{e,b}$ . Angles  $\alpha$  and  $\gamma$  (Fig. 4) can be expressed as

$$\alpha = \alpha_1 + \alpha_2 \quad (44)$$

$$\gamma = \gamma_1 + \gamma_2 \quad (45)$$

Then

$$CD^2 = AC^2 + AD^2 - 2AC \cdot AD \cdot \cos \alpha_1 \quad (46)$$

and according to Eq. (44)  $\alpha$ .

$$\cos \alpha_1 = \cos \alpha \cdot \cos \alpha_2 + \sin \alpha \cdot \sin \alpha_2 \quad (47)$$

while

$$\sin \alpha_2 = \frac{BC}{AC} \quad (48)$$

$$\cos \alpha_2 = \frac{AB}{AC} \quad (49)$$

and

$$AC^2 = AB^2 + BC^2 \quad (50)$$

Additionally

$$AB = x(t_{e,b}) = u_{dr_i}^x(0)\tau \ln \left( 1 + \frac{t_{e,b}}{\tau} \right) \quad (51)$$

$$BC = y(t_{e,b}) = \frac{(ur_{\text{term}}^y)^2}{g} \ln \left( \cosh \left( \frac{gt_{e,b}}{ur_{\text{term}}^y} \right) \right) \quad (52)$$

$$CD = u_{\max,dU_2} \cdot t_{e,b} \quad (53)$$

Then Eq. (45) becomes

$$\begin{aligned} u_{\max,dU_2}^2 \cdot t_{e,b}^2 - \left( x^2(t_{e,b}) + y^2(t_{e,b}) \right) - AD^2 \\ + 2\sqrt{x^2(t_{e,b}) + y^2(t_{e,b})} \cdot AD(\cos \alpha \cdot \cos \alpha_2 + \sin \alpha \cdot \sin \alpha_2) \\ = 0 \end{aligned} \quad (54)$$

In Eq. (54)  $\alpha$  and  $AD$  can be efficiently approximated, e.g. by using multilateral radar triangulation (MRT) [65] to geolocate the target. As a result, even though it is difficult to analytically solve Eq. (54) for  $t_{e,b}$ , an arithmetic solution is straightforward.

Then the innovative Algorithm 1 intercepts the G-B-KD. Algorithm 1 has two parts: initialization and interception. During initialization,  $dU_1$  and  $dU_2$  receive from the MRT, the speed and location of the G-B-KD and start moving towards it. Interception assumes that the G-B-KD releases the bomb. In this case and in parallel: (a)  $dU_2$  receives from the MRT parameters  $\alpha$  and  $AD$ , estimates the trajectory of the bomb as well as  $t_{e,b}$ , moves towards the interception location C, captures the bomb and lands at a safe area, (b)  $dU_1$  moves towards the G-B-KD and when it is close enough it releases the EMP. Then it receives from the MRT parameters  $\alpha$  and  $AD$ , estimates the trajectory of the bomb as well as  $t_{e,b}$ , moves towards the interception location C, captures the G-B-KD and lands at a safe area.

Here, the differences between the proposed method and Proportional Navigation (PN) are also emphasized, since PN is a guidance law that is predominantly used for homing missiles and aerospace interceptors. In PN even when the target does not maneuver, the pursuer follows a curved trajectory as it continuously adjusts its velocity to maintain the pursuit and minimize the Line-of-Sight (LOS). In contrast to PN, the proposed method follows a straight line (DC in Fig. 4). The straight line is the minimum distance (leading to the minimum interception time) between pursuer and target. On the other hand, the curved path provided by PN is not the minimum distance between pursuer and target and it does not lead to the minimum interception time. For small DA (Fig. 4) in the range of 5–10 m, interception times from PN and the proposed method are similar, but as DA increases the difference between interception times also increases. Here it should be mentioned that in the proposed scheme, DA depends on the power of the EMP weapon. In any case, the interception time of the proposed scheme is always less than the interception time of PN. Additionally, PN's results depend on a positive navigation constant, usually denoted by  $N_1$ . Different values of  $N_1$  provide different interception times. On the contrary, the interception time of the proposed scheme does not depend on the selection of any parameters. Finally, the



Algorithm 1: Generic Interception of G-B-KD

```

// ##### INITIALIZATION #####
if (MRT.detect > 0) // G-B-KD detected by MRT (multilateral radar triangulation) near C
then
{
  dU1.MRT_receive.location -> (xd(t), yd(t)) &
  & dU2.MRT_receive.location -> (xd(t), yd(t)) // dU1 and dU2 continuously
  receive estimated location of G-B-KD, where yd(t) = Hb
  dU1.MRT_receive.speed -> (udr1y(t), udr1x(t)) &
  & dU2.MRT_receive.speed -> (udr2y(t), udr2x(t)) // dU1 and dU2
  continuously receive estimated speed of G-B-KD
  dU1.move.to (xd(t), yd(t)) = true &
  & dU2.move.to(xd(t), yd(t)) = true // dU1 and dU2 go towards the target
}

// ##### BOMB & G-B-KD INTERCEPTION #####
if {G-B-KD.release_bomb == "true"} // G-B-KD releases bomb
then do in parallel
{
  { // running on dU2
    dU2.MRT_receive.parameters -> (ab, ADb) // dU2 receives a and AD of
    the bomb (ab, ADb) from MRT (Fig. 4)
    dU2.estimate -> (x(t), y(t)) // dU2 estimates trajectory of the bomb using
    Eq. (27) and Eq. (41)
    dU2.calculate -> te,b // dU2 calculates time to intercept bomb using Eq.
    (54)

    dU2.move.to -> C // dU2 goes to the bomb interception location (Fig. 4)
    dU2.use.netgun = true // dU2 releases net and captures bomb
    dU2.land.safe = true // dU2 & captured bomb land at safe area
  } // end running on dU2
  { // running on dU1
    dU1.MRT_receive.location -> (xd(t), yd(t)) // dU1 continuously receives
    estimated location of G-B-KD
    dU1.move.to (xd(t), yd(t)) = true // dU1 goes towards the G-B-KD
    dU1.MRT_receive.parameters -> (ADd) // dU1 continuously receives AD
    of the G-B-KD (ADd) from MRT (Fig. 4)
    if (ADd < EMP_thresh) // dU1 is close enough to G-B-KD
    then{
      dU1.use.EMP = true // dU1 releases EMP
      dU1.MRT_receive.parameters -> (ad, ADd) // dU1 receives a and
      AD of the G-B-KD (ad, ADd) from MRT (Fig. 4)
      dU1.estimate -> (x(t), y(t)) // dU1 estimates trajectory of the
      G-B-KD using Eq. (27) and Eq. (41)
      dU1.calculate -> te,b // dU1 calculates time to intercept G-B-KD
      using Eq. (54)
      dU1.move.to -> C // dU1 goes to the G-B-KD interception location
      (Fig. 4)
      dU1.use.netgun = true // dU1 releases net and captures G-B-KD
      dU1.land.safe = true // dU1 & captured G-B-KD land at safe area
    }
  } // end running on dU1
} // end do in parallel

```

computational complexity of PN is higher compared to the proposed scheme. In particular, in case of PN, the pursuer has to: (a) continuously estimate the LOS angular rate and the rate of change of the distance from the pursuer to the target and (b) adjust its path in order to intercept the target. On the contrary, Eq. (54) of the paper has to be arithmetically solved only once.

5. Experimental results

Experimental simulations and comparisons were carried out using a PC with Intel(R) Core i7-12700 CPU @ 3.60 GHz and 16 GB DDR4 RAM. R 4.3.1 was also incorporated.

Initially, a worst-case scenario is analyzed for ANFO, TNT and Octanitrocubane (Table 2). It is assumed that all G-B-KDs are rigged with ANFO, TNT or Octanitrocubane and carry one releasable bomb of the same substance. Here it should be mentioned that: (a) similar calculations are available for all substances of Table 2 and (b) based on each explosive's cost, it is likely that terrorists will use ANFO (~400 Euro/ton) [66], or TNT (~2000 Euro/ton) [67].

Octanitrocubane is unlikely to be used, since its base (dimethyl cubane-1,4-dicarboxylate) has a cost of about 36,000 Euro/kg [68], which is much higher than the cost of buying a non-military UAV or the cost of buying other weapons. According to the worst-case scenario, all G-B-KDs carry the maximum load (bomb + rigged explosives), as terrorists seek to maximize the overall impact of an attack. The maximum load for different non-military UAVs is provided in Table 5, while results are provided for six different masses:  $M_1 = 100$  kg,  $M_2 = 50$  kg,  $M_3 = 25$  kg,  $M_4 = 10$  kg,  $M_5 = 5$  kg, and  $M_6 = 1$  kg. Griff 800 (Table 5) has a maximum payload of 800 kg. This threat cannot be confronted by the proposed scheme, since it is extremely difficult to capture with a net, carry and land such a huge payload and further research should be carried out.

Fig. 5(a) (ANFO), 5(b) (TNT) and 5(c) (OCTANITROCUBANE) show overpressure (log10) versus distance (m) from a CI, for the six different masses ( $M_1$ - $M_6$ ) and for the following distances: 0.01 m (point-blank), 1 m, 2 m, 5 m, 10 m, 20 m, 40 m, 50 m, 100 m, 150 m, 200 m, 250 m, 300 m, 350 m, 400 m, 450 m, and 500 m. As it can be observed: (a) the maximum overpressure is 11,867.51 psi for  $M_1$  of Octanitrocubane at 0.01 m, (b) a bomb/G-B-KD explosion is very dangerous (psi > 1 - Table 1) for distances more than 50 and less than 100 m for 100 kg. In this case ANFO provides 1.16 psi (50 m) and 0.53 psi (100 m), TNT provides 1.31 psi (50 m) and 0.59 psi (100 m) and Octanitrocubane provides 1.95 psi (50 m) and 0.81 psi (100 m) and (c) the explosion is dangerous even for  $M_6$  and for distances 10 m–20 m. In this case ANFO provides 1.27 psi (10 m) and 0.57 psi (20 m), TNT provides 1.45 psi (10 m) and 0.64 psi (20 m) and Octanitrocubane provides 2.17 psi (10 m) and 0.88 psi (20 m).

For the next experiments and without loss of generality, it is assumed that the bomb is spherical ( $C_d = 0.47$ ) and it follows the ground burst condition, while the G-B-KD may follow either the ground or the air burst condition, before stricken by the EMP. After stricken by the EMP it can follow only the ground burst condition. Additionally,  $\rho_a = 1.204$  kg/m<sup>3</sup>,  $g = 9.81$  m/s<sup>2</sup>, while

$$A_b = \pi \cdot R^2 \tag{55}$$

where  $R$  is the radius of the sphere. Since six different bomb masses are considered, it is assumed that each sphere has a different radius, leading to the following six radius-mass couples: (0.05 m,  $M_6$ ), (0.1 m,  $M_5$ ), (0.13 m,  $M_4$ ), (0.20 m,  $M_3$ ), (0.25 m,  $M_2$ ) and (0.3 m,  $M_1$ ).

Furthermore, according to Table 5, the  $M_6$  mass can move at a top speed of 289 km/h (80.28 m/s), the  $M_5$  and  $M_4$  masses can move at 130 km/h (36.11 m/s), while the  $M_3$ ,  $M_2$ , and  $M_1$  masses can move at 100 km/h (27.28 m/s). Then, the bombs' trajectories for

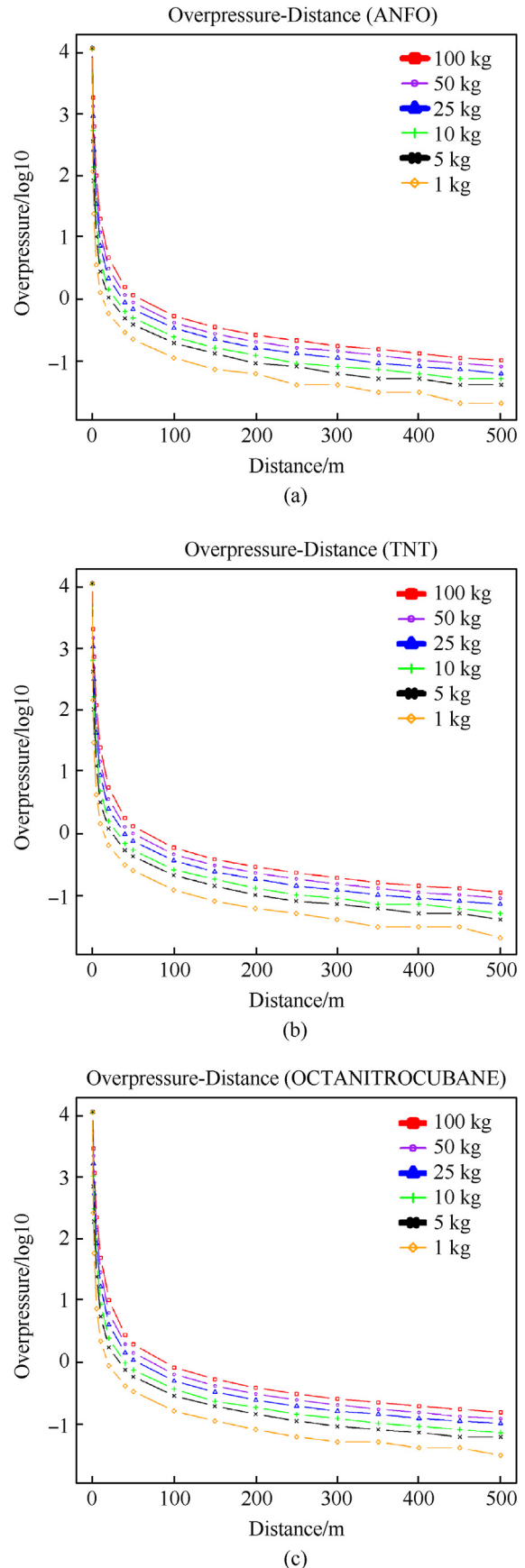
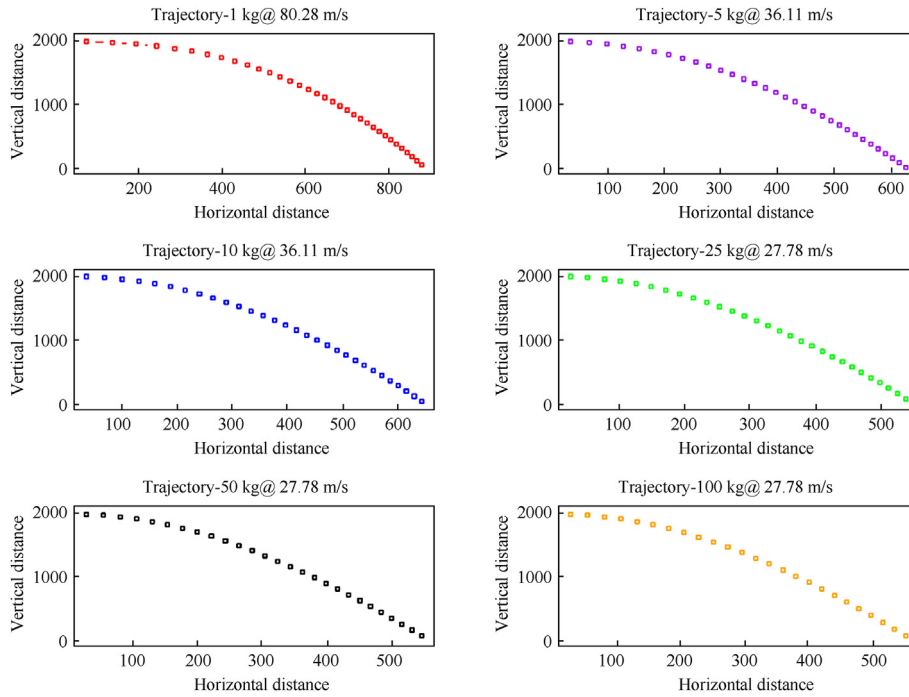


Fig. 5. Overpressure (log10) versus distance (m) for six different masses ( $M_1$ - $M_6$ ) and seventeen distances (0.01–500 m): (a) ANFO; (b) TNT; (c) Octanitrocubane.



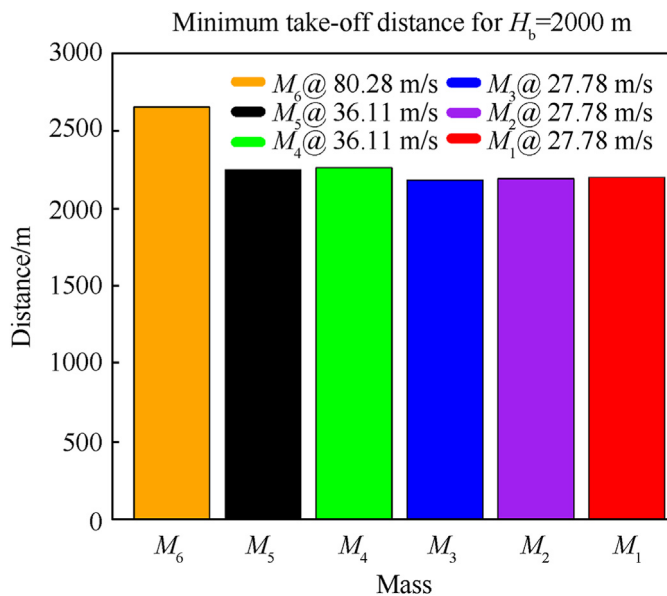
**Fig. 6.** Bomb trajectory for six different masses ( $M_1$ – $M_6$ ) with  $H_b = 2000$  m:  $M_6$  at 80.28 m/s (289 km/h),  $M_5$  at 36.11 m/s (130 km/h),  $M_4$  at 36.11 m/s (130 km/h),  $M_3$  at 27.28 m/s (100 km/h),  $M_2$  at 27.28 m/s (100 km/h) and  $M_1$  at 27.28 m/s (100 km/h).

$H_b = 2,000$  m are illustrated in Fig. 6. As it can be observed,  $M_6$  travels horizontally for about 880 m until it reaches the ground. The values for  $M_5$ ,  $M_4$ ,  $M_3$ ,  $M_2$ , and  $M_1$  are about 628 m, 643 m, 537 m, 546 m, and 552 m respectively. The times of flight are also different.  $M_6$  reaches the ground at about 34 s. The values for the other five masses are about 32 s, 30 s, 29 s, 27 s, and 25 s respectively. If the bombs are released from  $H_b = 50$  m, then, all of them reach the ground in less than 3 s.

According to the above results (Figs. 5 and 6), the couple of the

DDs should take off in time in order to successfully deal with the various threats. It is assumed that the DDs take off from the ground, matching the arrangements of Figs. 3 and 4. Additionally, due to the proposed modifications, it is assumed that the DDs could reach a top speed of 444 km/h, at a 5 g sustained acceleration (e.g. 20% less than the original Raytheon Coyote Block 2) [64,69].

Thus, they reach top speed in 9.05 s, covering a distance of 2008.66 m. After this distance, the DDs fly at top speed. Furthermore, it is assumed that  $H_b = 2000$  m and the G-B-KD flies at its top speed to reach a point, where it can release the bomb (release-point). The release-point is different for the different masses and it depends on two factors: (a) the trajectory of the bomb (covered horizontal distance – Fig. 6) and (b) the blast overpressure (Fig. 5). For example, in case of  $M_6$  at 80.28 m/s the horizontal distance is 880 m while the blast overpressure falls under one ( $\text{psi} < 1$ ) for distances over 20 m. In this case, the minimum horizontal distance to intercept the G-B-KD is 900 m (880 m trajectory + 20 m blast). Since  $H_b = 2000$  m, according to the Pythagorean theorem and solving for the hypotenuse, the Euclidean distance of the release-point to intercept the G-B-KD is 2193.17 m. Similar calculations were performed for  $M_5$  at 36.11 m/s,  $M_4$  at 36.11 m/s,  $M_3$  at 27.28 m/s,  $M_2$  at 27.28 m/s, and  $M_1$  at 27.28 m/s. Of course, the G-B-KD can release the bomb earlier, however, in this case the bomb will not damage the CI, but it may harm people and damage their properties (houses, cars etc.). In this paper it is assumed that the G-B-KD aims at damaging CIs, thus it tries to reach the release-point. However, if the mission of the G-B-KD is threatened by the DDs, it is assumed that it is programmed to release the bomb as close to the release-point as possible. Having estimated the release-point of the bomb and by knowing the top speed of the G-B-KD, the minimum distance, at which the DDs should take off can be estimated. For example, in case of  $M_6$  at 80.28 m/s, the DD reaches top speed at 9.05 s, having covered a distance of 2008.66 m. In order to reach the release-point (2193.17 m) it needs 1.5 more second and from take-off 10.55 s in total (9.05 s + 1.5 s). On the other hand, the G-B-KD covers a distance of 846.95 m in 10.55 s. It is assumed that the G-B-



**Fig. 7.** Minimum take-off distance for six different masses ( $M_1$ – $M_6$ ) with  $H_b = 2000$  m: (a)  $M_6$  at 80.28 m/s (289 km/h); (b)  $M_5$  at 36.11 m/s (130 km/h); (c)  $M_4$  at 36.11 m/s (130 km/h); (d)  $M_3$  at 27.28 m/s (100 km/h); (e)  $M_2$  at 27.28 m/s (100 km/h) and (f)  $M_1$  at 27.28 m/s (100 km/h).



KD moves horizontally, since its flying height is crucial to succeed to its mission. As a result, the DDs should take-off when the horizontal distance of the G-B-KD is 1746.95 m (900 m + 846.95 m). Solving again for the hypotenuse, the minimum distance of the G-B-KD from the CI at which the DDs should take-off is calculated. In the examined case, the distance is 2.655,33 m.

Fig. 7 provides the minimum take-off distances for all six masses ( $M_1$ – $M_6$ ) and for their respective speeds. As it can be observed the six couples of mass-take-off distance are: ( $M_1$ , 2199 m), ( $M_2$ , 2191.95 m), ( $M_3$ , 2183.73 m), ( $M_4$ , 2259.53 m), ( $M_5$ , 2246.93 m), and ( $M_6$ , 2655.33 m). Here it should be mentioned that the distance for  $M_1$ ,  $M_2$ , and  $M_3$  at 27.78 m/s slightly decreases, due to the decrease of the mass, since  $\tau$  increases with mass (Eq. (41) and (35)). Similar observations apply to  $M_4$  and  $M_5$  at 36.11 m/s.

### 5.1. Comparison to state-of-art

In this subsection, the proposed approach is compared to the following state-of-art approaches: (a) LM: loitering munition (exploding UAV) [70], (b) DUNnE: DD with net, without EMP [43,47,48,50], (c) DUNE: DD with net and EMP. It is also assumed that the aforementioned compared DDs do not include the proposed innovative point-of-interception computational method, but use the very common Go-onto-target (GOT) guidance system [71] to follow the target, during the phase of free fall with air resistance. More specifically, a semi-active radar homing (SARH) is assumed to be adopted by the three compared schemes. The SARH combines a passive radar receiver on the DD with a separate targeting radar that marks the target. SARH is the most common guidance solution for ground- and air-launched anti-aircraft systems [72].

Before providing experimental results, the following points are made: (a) in all approaches it is assumed that the DDs fly at top speed to approach the target, (b) in all approaches it is assumed that the DDs are not on a collision course with the targets, but chase the targets by following their tails, (c) LM explodes when its distance from the target is less than 5 m, (d) DUNnE approaches the target to less than 5 m and releases the net after keeping this distance for about  $t_{r1}$  s (reducing probability to miss the target), where  $t_{r1}$  depends on the mass of the target, (e) DUNE approaches the G-B-KD to less than 5 m and releases the EMP, causing the G-B-KD to start its free fall with air resistance. Then DUNE approaches the target to less than 5 m and releases the net, after keeping this distance for about  $t_{r2}$  s, (f) in this paper  $t_{r1} > t_{r2}$ , since DUNnE does not use EMP to interrupt the autonomous flight of the target. As a result, the G-B-KD may change its flight characteristics (speed, acceleration, direction etc.) at any time. Thus, DUNnE waits for a little more before releasing the net, to increase the success of capturing the target.

In the following experiments  $t_{r1}/t_{r2}$  is set to  $3/2 \pm 10\%$  s for  $M_1$ ,  $M_2$  and  $M_3$  and to  $2/1 \pm 10\%$  s for  $M_4$ ,  $M_5$  and  $M_6$ . The  $\pm 10\%$  provides some flexibility to the estimations, in order to cover most cases. Threshold  $t_{r2}$  is also used by the proposed scheme. Fig. 8 provides the time to neutralize the target, for all six masses ( $M_1$ – $M_6$ ) and for initial distances from 50 m to 800 m.

The initial distance ( $AD$  – Fig. 4) is the Euclidian distance between  $dU_2$  and the mass at  $t = 0$  (bomb released at  $t = 0$  from height  $H_b$ ). In Fig. 8, the scale of x-axis (time) is 1/10 of a second. As it can be observed, LM provides better results than DUNnE and DUNE. Compared to the proposed scheme: (a) in case of  $M_6$ , LM performs better only for an initial distance of 50 m. For more than 50 m the proposed scheme provides better performance, (b) in cases of  $M_5$  and  $M_4$  LM performs better for initial distances up to 250 m. For more than 250 m the proposed scheme provides better performance, (c) in case of  $M_3$ , LM performs better for initial distances up

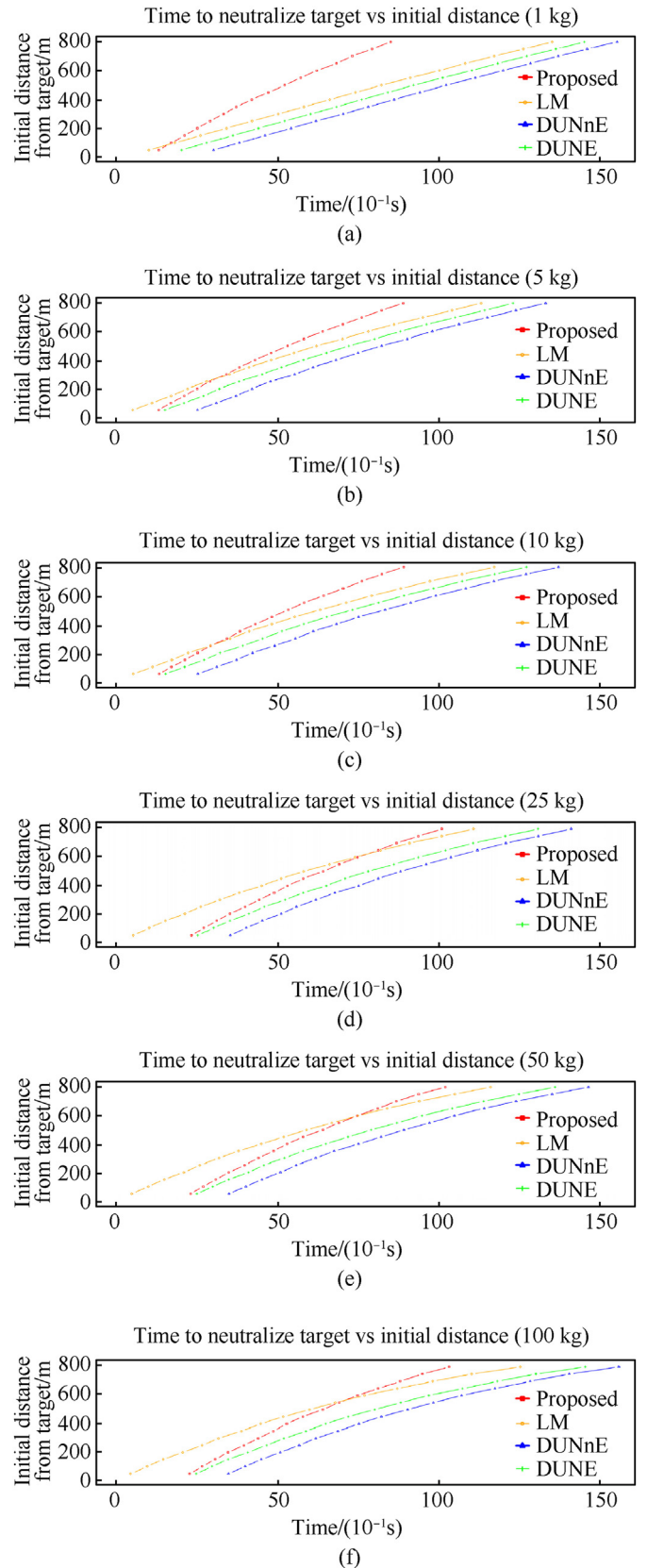


Fig. 8. Time to neutralize target for different initial distances (50 m–800 m): (a)  $M_6$  at 80.28 m/s, (b)  $M_5$  at 36.11 m/s, (c)  $M_4$  at 36.11 m/s, (d)  $M_3$  at 27.28 m/s, (e)  $M_2$  at 27.28 m/s, and (f)  $M_1$  at 27.28 m/s.

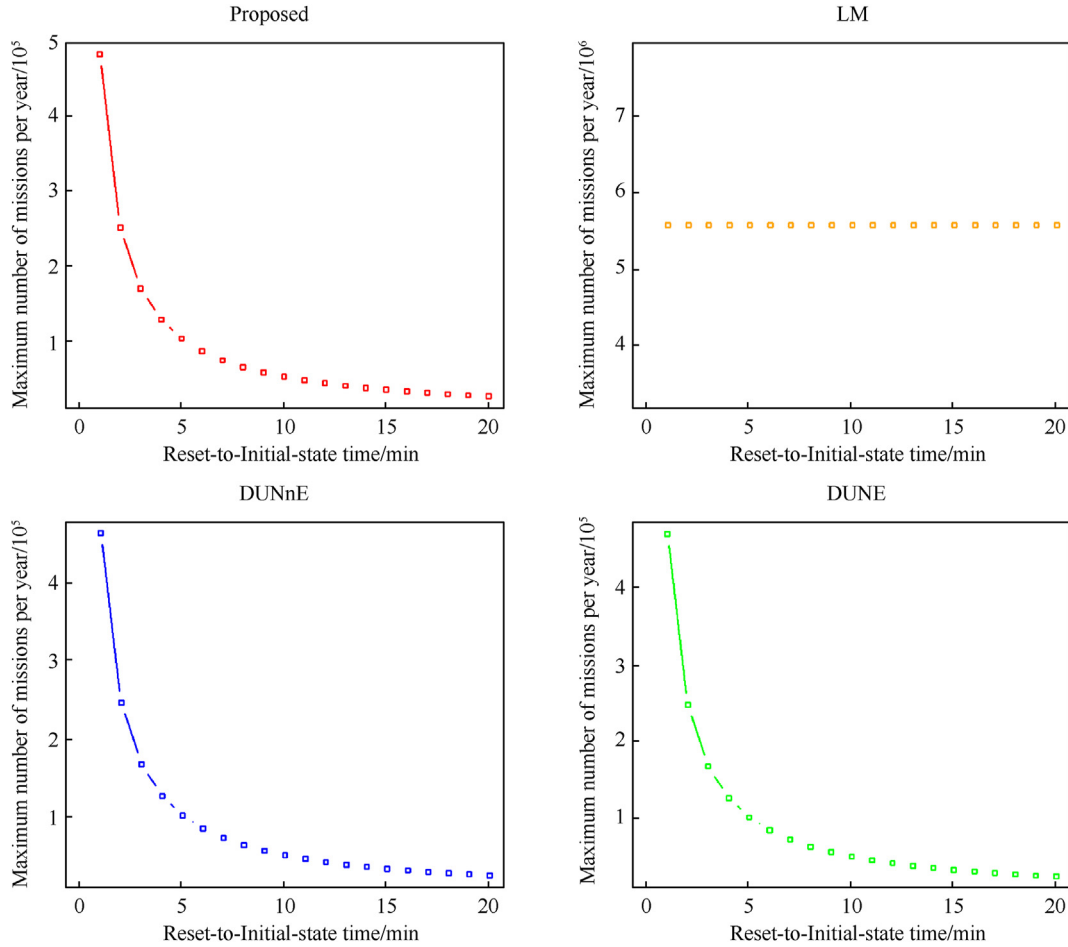


Fig. 9. Maximum number of missions per year for different reset-to-initial-state times.

to 600 m. For more than 600 m the proposed scheme provides better performance and (d) in cases of  $M_2$  and  $M_1$  LM performs better for initial distances up to 550 m. For more than 550 m the proposed scheme provides better performance. Overall, the proposed scheme provides an average time to neutralize target of 5.27 s, while LM provides 5.66 s, DUNnE provides 8.16 s and DUNE provides 7.16 s respectively. Thus, on average, the proposed scheme needs less time to neutralize the target, even though LM explodes when it approaches the target to less than 5 m. This is due to the fact that the proposed scheme incorporates the proposed innovative method to estimate the optimal points of interception (Fig. 4 and Eq. (54)), while LM, DUNnE and DUNE follow the tail of the target (full trajectory). As a result, on average, the proposed scheme provides a time reduction of 6.89%, 35.42% and 26.4% compared to LM, DUNnE and DUNE respectively, in case the target is on free fall with air resistance.

Regarding the operational capacity of each scheme, the maximum number of missions per year is estimated. More specifically, it is assumed that a mission starts at  $t = 0$  (bomb release) and ends when  $dU_1$  and  $dU_2$  are ready for the next take-off. The total time or reset-to-initial-state time ( $T_t$ ) includes the time to take-off and approach targets ( $t_{ap}$ ), the time to neutralize targets ( $t_n$ ), the time to land at the safe area ( $t_{ln}$ ), the time to fill up fuel ( $t_{fl}$ ) and the time to be put on the launcher for the next launch ( $t_l$ ):

$$T_t = t_{ap} + t_n + t_{ln} + t_{fl} + t_l \quad (56)$$

If we set

$$T_r = t_{ap} + t_{ln} + t_{fl} + t_l \quad (57)$$

Then  $T_t$  can be written as

$$T_t = T_r + t_n \quad (58)$$

Additionally,  $t_n$  is replaced by the average time to neutralize targets, which has been previously estimated (Fig. 8) and

$$ET_r = \{T_r \in \mathbb{N} : 1 \leq T_r \leq 20\} \quad (59)$$

where  $ET_r$  is the set of the different integer values that  $T_r$  receives. In the following results, the minimum value is 1 min and the maximum is 20 min. Fig. 9 illustrates the maximum number of missions per year for the four compared schemes.

As it can be observed: (a) LM provides a fixed maximum number of missions per year (5,571,731), since  $T_r$  equals to zero. However, since the DDs explode, the new mission should be carried out by a new couple of DDs in case of LM (b) for the proposed approach and in case of  $T_r = 1$ , the maximum number of missions per year is 483,162, while for  $T_r = 20$ , the maximum number of missions per year falls to 26,165, (c) for DUNnE and in case of  $T_r = 1$ , the maximum number of missions per year is 462,676, while for  $T_r = 20$ , the maximum number of missions per year falls to 26,102 (d) finally for DUNE and in case of  $T_r = 1$ , the maximum number of missions per year is 469,565, while for  $T_r = 20$ , the maximum number of missions per year falls to 26,124. On average, the

proposed scheme reaches 91,089 maximum missions per year, while DUNnE and DUNE reach 89,364 and 89,948 maximum missions per year respectively. As a result, on average, the proposed scheme provides a maximum mission increase of 1.93% and 1.27% compared to DUNnE and DUNE respectively.

In the last experiment, the cost for different numbers of attacks is estimated for all schemes. Towards this direction let us assume that each DD has a weight of 10 kg and costs 10,000 Euros [73], except of the DD in case of LM, which costs 4000 Euros [74]. A lower cost is assumed, since in case of LM, the DD explodes and thus, it does include all special components that the DDs of the other three approaches are equipped with. Additionally, it is assumed that the DDs fly at top speed (444 km/h – 20% less than [64]). Let us also recall that the proposed scheme provides an average time to neutralize target of 5.27 s, while LM provides 5.66 s, DUNnE provides 8.16 s and DUNE provides 7.16 s respectively. Furthermore, let us assume that the rest of the mission (take-off, chase, land) requires 20 s on average, except in case of LM, which requires 10 s on average, since DDs do not land. Thus, on average, the total mission time is 25.27 s for the proposed scheme, 15.66 s for LM, 28.16 s for DUNnE and 27.16 s for DUNE. The major costs of each mission are: (a) the cost of buying the DDs, in case of LM and (b) the cost of the consumed fuel in all cases. In this paper, the theoretical thrust-specific fuel consumption (TSFC) [75,76] is adopted, were different TSFCs (different fuel efficiencies) are considered from 0.5 to 2.

Thrust is a mechanical force, generated through accelerating a mass of gas. The gas is propelled rearward, causing the engine to accelerate in the opposite direction [77]. In our case, each DD should produce a thrust to overcome two forces: (a) the weight force (Eq. (9)) and (b) the drag force Eqs. (6) and (28)). Thus

$$Th_d = m_d g + \frac{1}{2} \rho_a C_d A_b (u_d^{\max})^2 \quad (60)$$

where  $Th_d$  is the thrust,  $m_d$  is the mass and  $u_d^{\max}$  is the top speed of the DD. Here it should be mentioned that  $Th_d$  is estimated for  $u_d^{\max}$ . It should also be mentioned that it fluctuates based not only on the speed but also on the acceleration of the DD. However, Eq. (60) provides a good estimate of thrust, for a large part of the mission. Based on Eq. (60),  $Th_d = 233.23 \text{ N} = 23.78 \text{ kg}$  (force). Then, for example, if  $TSFC = 1.0/2.0$  then each DD needs 23.78/47.56 kg of fuel per hour (66.1/132.2 g/s). Raytheon Coyote Block 2 consumes JP-10 (exo-tetrahydrodicyclopentadiene, C10–H16), which is a synthetic aviation turbine fuel with an estimated cost of about 5300 Euro per ton (0,53 cents/g) [78]. Considering 10 missions per day on average,

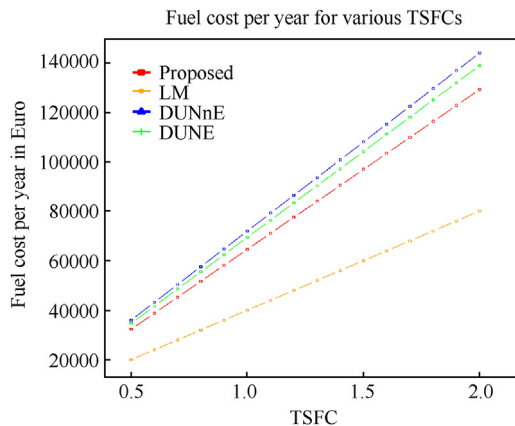


Fig. 10. Fuel cost in Euro per year for the various schemes.

to protect all the CIs of a country, the total number of missions per year is 3650. Fig. 10 illustrates the fuel cost per year for the compared schemes and for different TSFCs (from 0.5 to 2.0). As it can be observed, the minimum fuel cost per year (20,024.5 Euro) is achieved by LM, for  $TSFC = 0.5$ , while the maximum fuel cost (144,033.3 Euro) is achieved by DUNnE, for  $TSFC = 2.0$ . On average, the proposed scheme achieves a fuel cost of 80,782.2 Euro, while LM, DUNnE and DUNE achieve 50,061.3 Euro (38.03% less than the proposed), 90,020.8 Euro (11.44% more than the proposed) and 86,824 Euro (7.48% more than the proposed) respectively. Here it should be mentioned that LM provides lower fuel costs, since the DDs explode and thus, they do not land at a safe area, as it happens with the other schemes.

Finally, in order to take into consideration also the cost of buying the DDs, let us assume that each DD has an operating life of 1000 missions. In other words, after this threshold, the DD is withdrawn from operation. Additionally, in case of LM, in each mission two DDs are destroyed. Furthermore, it is assumed that there are not any other maintenance costs during the span of the operating life of the DDs.

Fig. 11 illustrates the total cost in Euro per 1000 missions for different TSFCs (from 0.5 to 2.0). As it can be observed, the minimum total cost (18,852.8 Euro) is achieved by the proposed scheme for  $TSFC = 0.5$ , while the maximum total cost (8,021,944.7 Euro) is achieved by LM for  $TSFC = 2.0$ . On average, the proposed scheme achieves a total cost of 32,132.1 Euro, while LM, DUNnE and DUNE achieve 8,013,715.4 Euro (24,839.91% more than the proposed), 34,663.2 Euro (7.88% more than the proposed) and 33,787.4 Euro (5.15% more than the proposed) respectively. It is obvious that the total cost of LM is extremely high and other solutions should be examined. For example, instead of exploding near the target, the DDs could fire projectiles [46] or rockets [79]. Finally, it should be stated that the proposed scheme provides an average cost of 32.13 Euro per mission, which is very reasonable if we take into consideration that multi-million CIs are protected.

## 6. Discussion and future work

Before closing this paper, some interesting aspects are discussed. The first is related to the number of required DDs to neutralize malicious drones. In particular, the proposed method requires 2 DDs for 1 malicious bomb-carrying, kamikaze drone. The malicious bomb-carrying, kamikaze drone is also rigged with explosives. If the malicious kamikaze drone and/or the bomb hit the CI they may cause severe damage. Thus, both the malicious kamikaze drone and the bomb should be neutralized. In other words, 2 DDs neutralize 2 threats, leaving a "clear ground" i.e. scattered fragments, remains, or pieces do not fall on the ground. In the ideal case, the malicious bomb-carrying, kamikaze drone does not release the bomb. In this case  $du_1$  is enough to neutralize the threats without the need of  $du_2$ . However, this case is very unlikely. Additionally, when a malicious bomb-carrying, kamikaze drone approaches a CI, no one can guarantee that it will not release the bomb. If the bomb is released, there are two "clear ground" options, using the minimum number of DDs: (a) the proposed approach and (b) another approach that uses only one DD, e.g.  $du_1$ . In the latter approach,  $du_1$  should capture the malicious kamikaze drone and then capture the bomb or capture the bomb and then the malicious kamikaze drone, before they reach the ground. Let us assume that  $du_1$  first captures the bomb and then chases the malicious kamikaze drone. If the captured bomb is detonated, it may destroy  $du_1$  and then the malicious kamikaze drone can head to the undefended CI. In any case, the latter approach needs further examination and triggers future research.

On the other hand, according to Eq. (56) of the paper, the



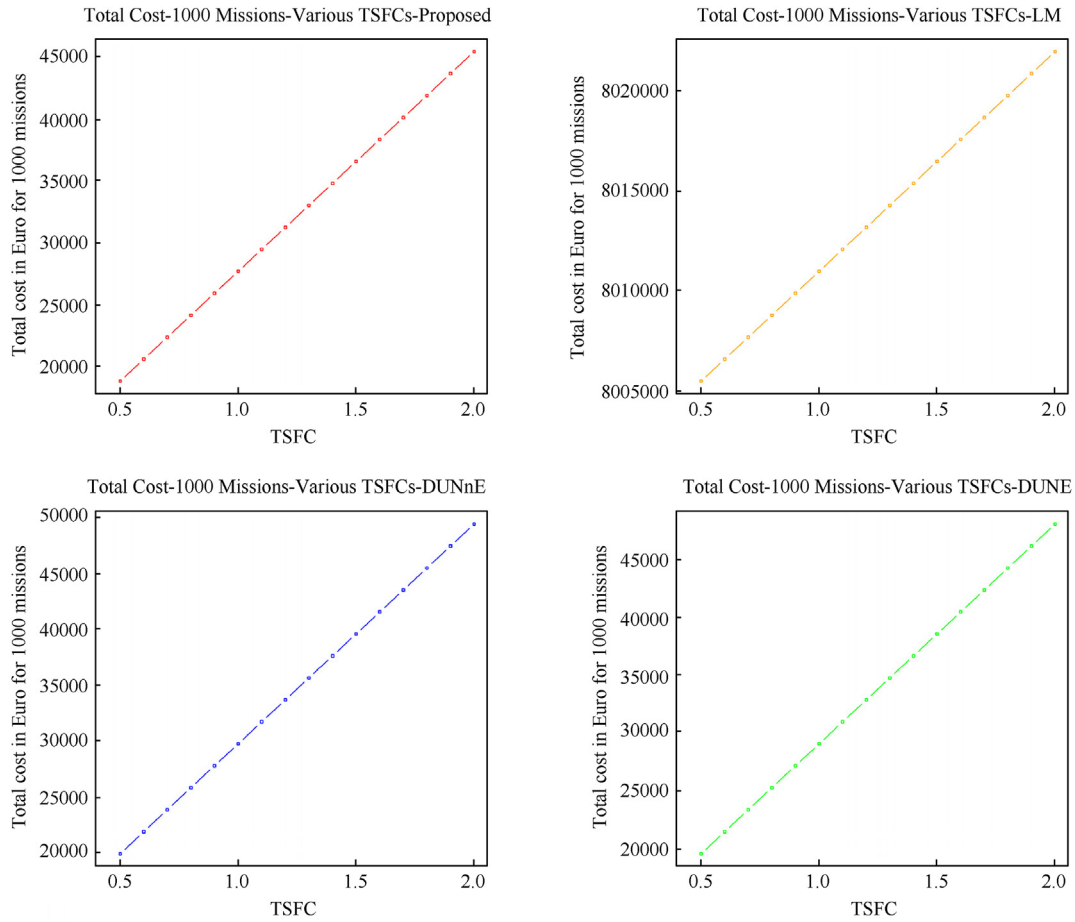


Fig. 11. Total cost in Euro per 1000 missions for the various schemes.

minimum total time of the proposed scheme ( $T_t$ ) is 65.27 s ( $T_r = 60$  s,  $t_n = 5.27$  s). In this case, if a swarm of consecutive malicious bomb-carrying, kamikaze drones arrive one-by-one at least every 65.27 s, then  $dU_1$  and  $dU_2$  can neutralize all of them. Thus, only 2 defensive drones ( $dU_1$  and  $dU_2$ ) are enough to protect the CI from a swarm of many consecutive malicious bomb-carrying, kamikaze drones. Another very interesting scenario that can be the focus of future research, is the case of a swarm of many non-consecutive malicious bomb-carrying, kamikaze drones that approach the CI all-together. In this case, the minimum horizontal interception distance can be increased (leading possibly to more false alarms). In any case, this scenario also triggers much future research.

It should also be stressed that Israel's Iron Dome and Raytheon Coyote Block 3 with EMP may efficiently confront the swarm of many non-consecutive malicious bomb-carrying, kamikaze drones, but they do not leave a "clear ground", a factor that is important in urban areas, where people and property should also be protected from sky-falling debris.

The second aspect focuses on behavioral changes of the kamikaze drones. More specifically: what happens if the kamikaze drones change their preset autonomous navigation algorithms when they detect a DD is approaching? Or what if the kamikaze drones change their goal of achieving maximum damage?

Changing of the kamikaze drones' preset autonomous navigation algorithms when they detect an approaching DD, is a very interesting case. The DDs surveil a specific geographical region (3D spatial volume) around the CI, the borders of which are determined

by the minimum take-off distance, as described in the paper. If the kamikaze drone crosses the border of the 3D spatial volume and continuous moving inside this volume, the DDs take-off and neutralize the kamikaze drone and the bomb. However, if the kamikaze drone enters the 3D spatial volume and after the DDs take-off the kamikaze drone exits the 3D spatial volume, this is a problem that needs to be analyzed in future research. Should the DDs intercept any drone even outside the 3D spatial volume, just because it has entered (maybe by mistake) the 3D spatial volume and exited before being neutralized? Should the DDs intercept drones even outside the 3D spatial volume, because they continuously enter and exit the volume (probably testing the protection algorithms of the DDs)? This case includes different subcases: (a) a testing-drone enters and exits the 3D spatial volume once (b) a testing-drone enters and exits the 3D spatial volume once and repeats this process after times  $t_1, t_2, t_3$ , etc., (c) a swarm of drones enter and exit the 3D spatial volume once, (d) a swarm of drones enter and exit the 3D spatial volume once and repeat this process after times  $t_1, t_2, t_3$ , etc. In these cases, probably drone-authentication methods should be incorporated to detect and confront testing-drones. In all cases, the DDs take-off, meaning that they consume fuel, their time until next service reduces and the CI may be vulnerable if it is attacked by the opposite direction.

On the other hand, changing of the kamikaze drones' goal of achieving maximum damage is another very interesting case. According to the proposed scheme, the DDs are programmed to take-off at the right moment to prevent any damage of the CI (minimum take-off distance from the CI, which determines the borders of the

3D spatial volume under surveillance). Even if the kamikaze drones' goal changes, they cannot approach the CI at a distance that will enable them to cause damage. Of course, a kamikaze drone can release the bomb at any time or can crash at any other location. However, in this case the bomb/kamikaze drone will not damage the CI, but may harm people and damage properties (houses, cars etc.) that are nearby the CI. It is very important to protect people and properties and future work should be carried out to examine schemes that can protect a whole city, leaving – at the same time – a "clear ground".

Future work can also focus on the case of very large payloads that cannot be effectively tackled by nets. Furthermore, another interesting case is when the kamikaze drone carries several releasable bombs. Additionally, CI-optimized security plans could be implemented, since each CI has different characteristics (size, dimensions, number of sensitive locations, level of importance, surrounding area etc.).

Finally, it should be mentioned that it is more practical to consider the drones' trajectories in 3 dimensions, even though the 2D motion provides a solution without loss of generality. The main reasons to consider 2D motion in this paper were to save space, use less formulas and less symbols, since the motions on  $x$  and  $z$  planes are described by similar mathematics.

## 7. Conclusions

CIs can be rapidly eliminated at a minimal expense, if aerial threats are not efficiently confronted. This work focused on the novel and under-researched field of neutralizing a fully autonomous, GPS-denied, bomb-carrying, non-military kamikaze drone. Towards this direction, this paper introduced the defensive couple of drones, which were equipped with a net-gun, with an innovative point-of-interception computational method and with an electromagnetic pulse weapon. Extensive results and comparisons to state-of-art methods, exhibited the advantages and limitations of the proposed scheme and triggered future work.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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