

# Sales and Promotions and the Great Recession Deflation

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# Introduction

## Motivation



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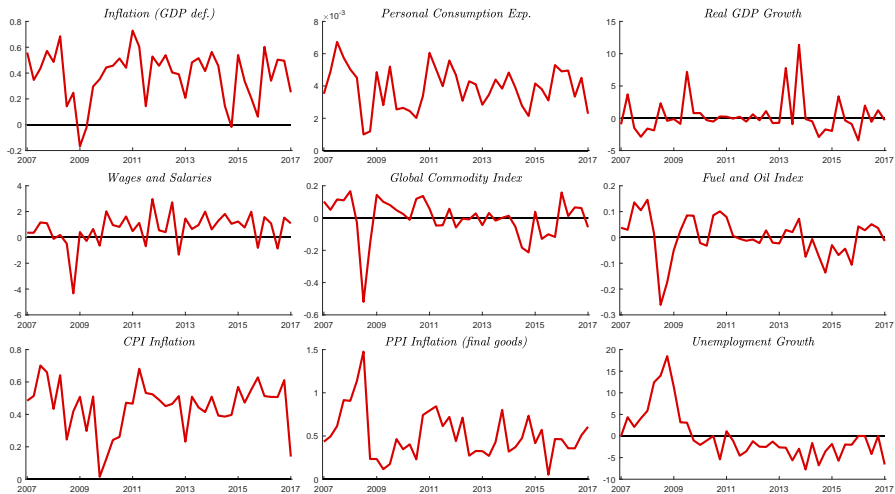
# Inflation Measures and the Phillips Curve

## Motivation

- Consumer price inflation, (personal consumption expenditures price index), was 2% between 2003 and 2007
- It only declined to 1.5% for the next 8 years, through the deepest contraction since the Great Depression (Gilchrist et al. 2017)
- It even casts doubt on the relevance of the Phillips curve relationship.
- Explanations involve the anchored expectations hypothesis or alternative definitions of economic slackness or even the financial accelerator
  - ▶ Ball and Mazumder (2011); Gordon (2013); Krueger, Cramer, and Cho (2014); Coibion and Gorodnichenk (2015); Del Negro, Giannoni, and Schorfheide (2015) and others

# Growth rates (Price Indices)

From St. Louis FRED



# Main Findings

## Main Goal

- We provide a different explanation as we show theoretically that occasional sales can have a significant effect in the cyclicity of price indexes.
- A theoretical model is provided where firms post sales on products infrequently.
- We report that price indexes that disregard sales are less volatile and more persistent than they would otherwise be.
- Moreover, when agents form expectations using indices net of sales, recessions are exacerbated.
- Infrequent Sales do not affect the inflation measures if the economy is at steady state.



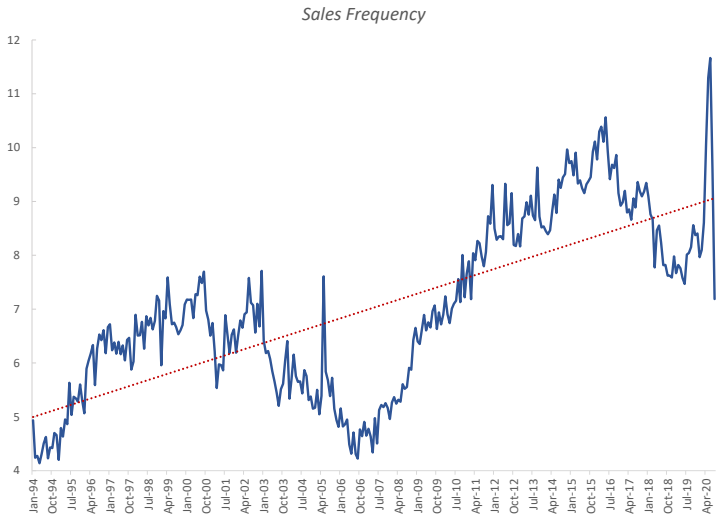
# Main Findings

## Main Goal

- We demonstrate that in a recession:
  - ▶ Sales become more generous
  - ▶ Sales are more frequent
  - ▶ Consumers devote more effort in identifying those bargains
- We re-estimate a simple Phillips curve relationship
  - ▶ We find that the UK CPI inflation with a higher weight on sale items correlates better with output gap and unemployment
  - ▶ The traditional CPI inflation is uncorrelated with output gap and unemployment as in Galí and Gertler (1999).

# Frequency of Sales

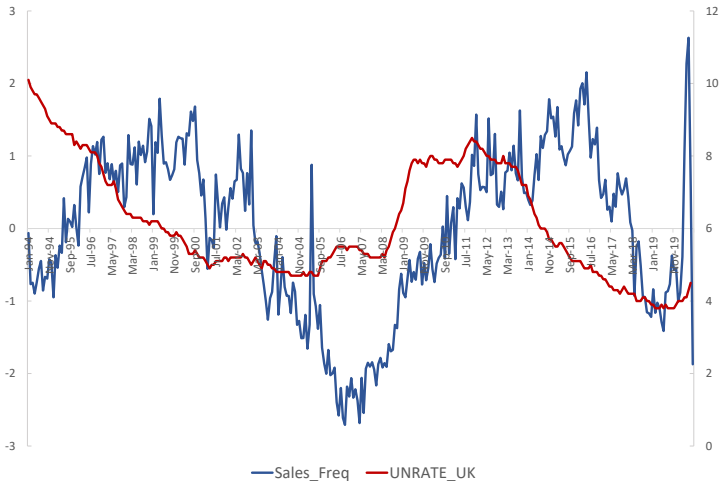
Relative number of goods on sale



# Frequency of Sales and Unemployment

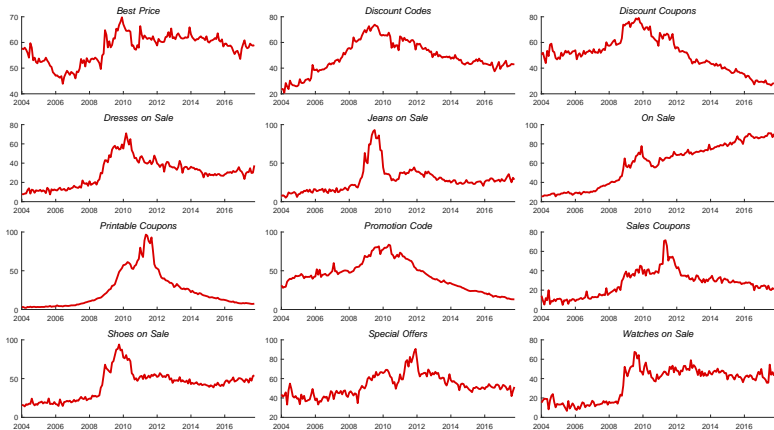
Relative number of goods on sale and Unemployment

*Sales Frequency vs Unemployment Rate*



# Popularity in various Google searches across time

## Sales Hunting

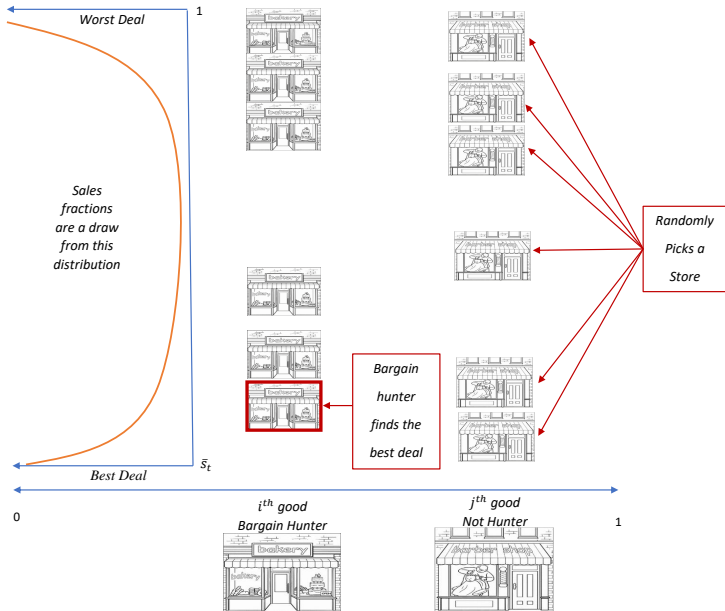


# Methodology

## The Model

- A Standard New Keynesian Model is modified with occasional sales
- Prices  $p_{it}$  are subject to menu costs
- Sales  $s_{it} \in [\bar{s}_t, 1]$  and thus the price paid by consumers for the  $i^{th}$  good is  $s_{it}p_{it}$ .
- Sales are unpredictable and are a draw from an endogenous distribution of sales. (similar to Varian (1980))
- Households send  $V_t$  share of consumers to search for bargains and  $1 - V_t$  randomly pick a store.
- The true price index in the economy is:

$$P_t = \left[ \begin{aligned} & (1 - V_t) (p_{it})^{1-\theta} \int_{\bar{s}_t}^1 (s_{it})^{1-\theta} f(s_{it}) ds_{it} \\ & + V_t (p_{it})^{1-\theta} \int_{\bar{s}_t}^1 (s_{jt})^{1-\theta} (1 - F(s_{jt}))^{N-1} f(s_{jt}) ds_{jt} \end{aligned} \right]^{\frac{1}{1-\theta}}$$



# The Model

## Firms

- There is no equilibrium in pure strategies in this model but there is one in mixed strategies.
- $F(s_t) \equiv \Pr(s_{it} < s_t)$  for  $i \in \{1, 2, \dots, N\}$  is the probability the  $i^{\text{th}}$  producer to have a lower sale fraction than  $s_t$
- The Profit for a firm is

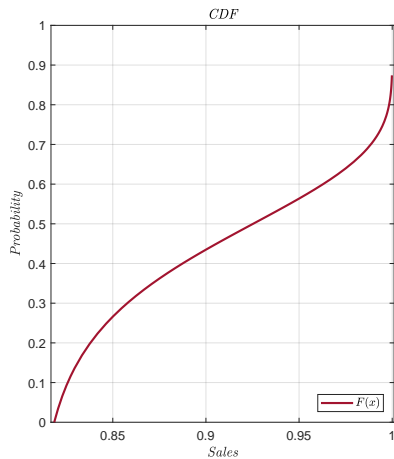
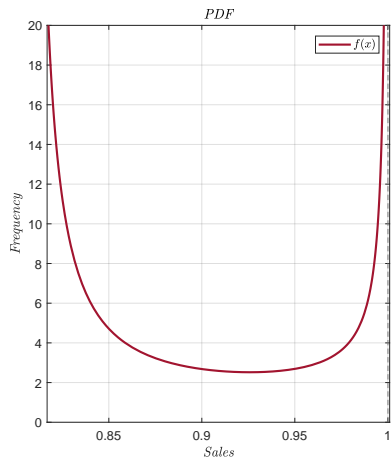
$$\Xi(s_t) = \Pi_t^V(s_t) (1 - F(s_t))^{N-1} + \Pi_t^{NV}(s_t) \left(1 - (1 - F(s_t))^{N-1}\right)$$

- In mixed strategies any  $s_t \in [\bar{s}_t, 1]$  should give the same expected profit to the firm.
- Therefore,  $\Xi(s_t) = \Xi(1)$
- From this, the distribution of sales can be identified:

$$F(s_t) = 1 - \left[ \frac{1 - V_t}{V_t} \frac{1}{N} \left( \frac{\frac{p_t}{P_t} - m_t}{s_t \frac{p_t}{P_t} - m_t} s_t^\theta - 1 \right) \right]^{\frac{1}{N-1}}$$

- Differentiating gives the pdf:  $f\left(s_t; N, V_t, \frac{p_t}{P_t}, m_t\right) = \frac{dF(s_t)}{ds_t}$

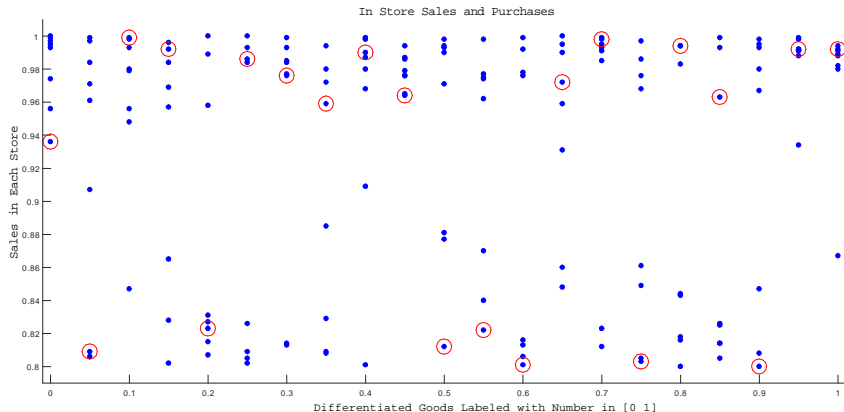
# The PDF and CDF of Sales





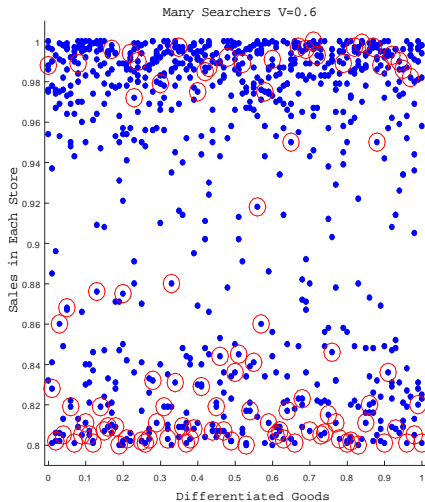
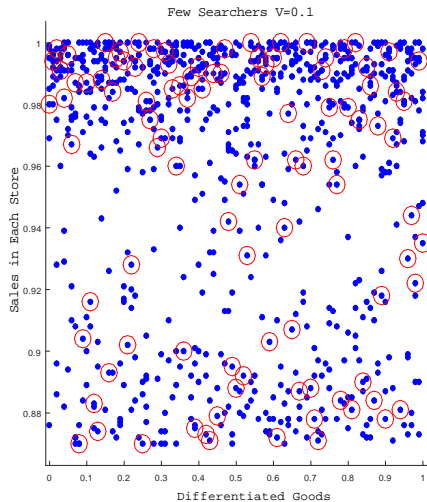
# An Example of Realized Sales by store

Circles are the choices by a household with 0.5 of members as bargain hunters



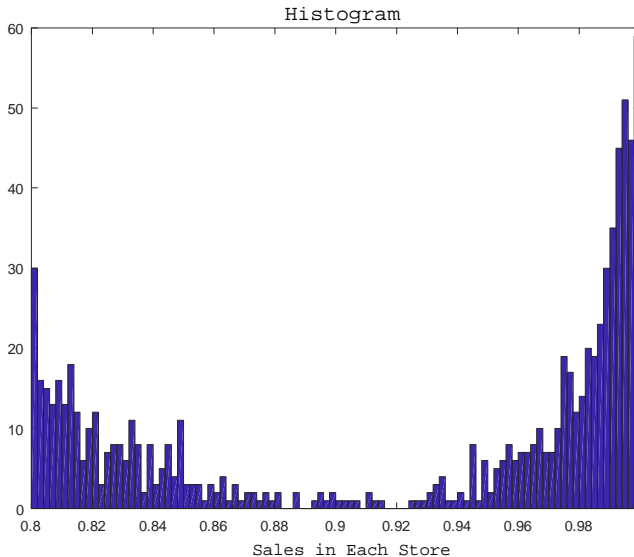
# Sales and Prices in Recession

Shows how prices paid by customers change during recessions

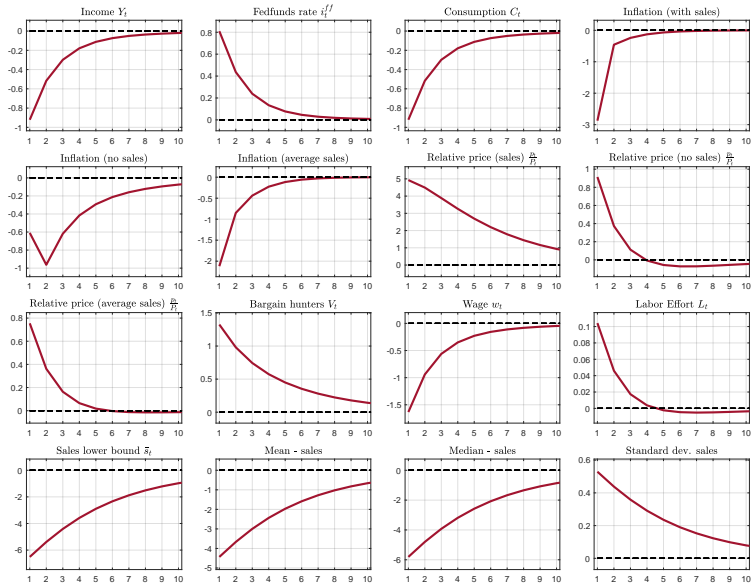


# The histogram From the Previous Example

Captures the Distribution of Sales

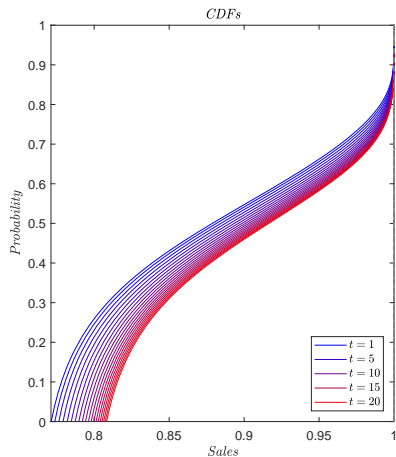
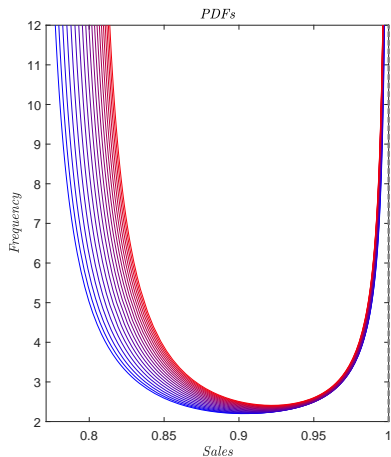


# IRFs after a 1 sd Increase in Federal Funds Rate

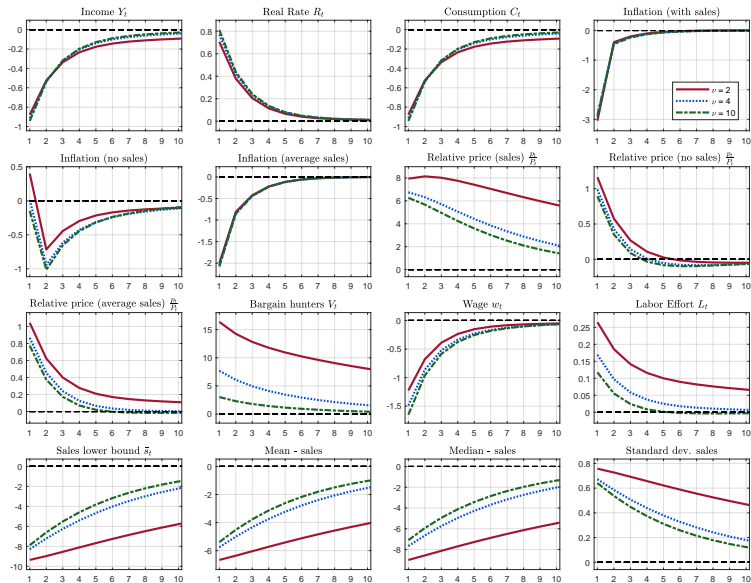


# Dynamic Distribution of Sales after 1 SD Increase in Federal Funds Rate

Movement from red to the rightmost blue line



# IRFs after a 1 sd Increase in Federal Funds Rate



# Taylor Rule

## The Importance of Persistence

- The log-linear Euler equation is:

$$\hat{y}_t = E_t \hat{y}_{t+1} - (i_t - E_t \pi_{t+1}) \quad (1)$$

where  $\hat{y}_t$  is the log deviation of output  $Y_t$  from its steady state,  $\pi_t$  the inflation and  $i_t$  the log linearized gross nominal rate from its steady state.

- The log-linearized Taylor rule according to which the central bank sets the interest rate is

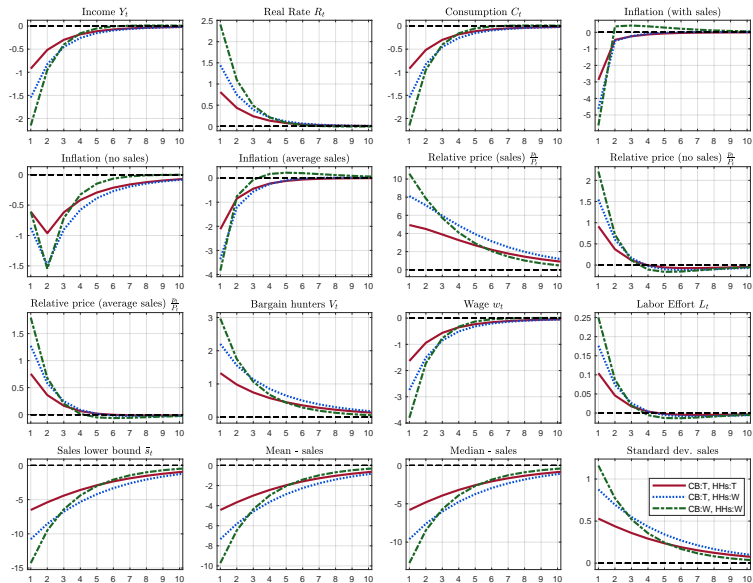
$$i_t = \rho^i i_{t-1} + (1 - \rho^i) (\rho^\pi \pi_t + \rho^y \hat{y}_t)$$

- Solving equation (1) forward implies

$$\hat{y}_t = - \sum_{i=0}^{\infty} E_t (i_{t+i} - E_t \pi_{t+i+1})$$

- The deviation of current income from steady state is the sum of all deviations of future real interest rates from steady state.

# IRFs after a 1 sd Increase in Federal Funds Rate





# Empirical Exercise

## Phillips Curve Estimation

Dependent variable:  $\pi_t$  CPI

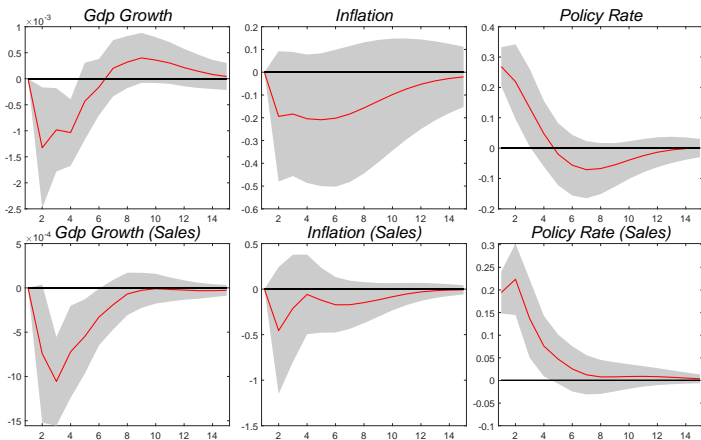
	Model 1	Model 2	Model 3	Model 4
Constant	5.974* (3.203)	5.457* (3.326)	2.782*** (0.707)	2.763*** (0.689)
Inflation $\pi_{t-1}$	0.055 (0.109)	0.055 (0.110)	0.079 (0.097)	0.082 (0.090)
Output gap $x_t$			0.008 (0.009)	
Output gap $x_{t-1}$				0.007 (0.008)
Unemp. rate $u_t$	-0.498 (0.410)			
Unemp. rate $u_{t-1}$		-0.413 (0.431)		

Dependent variable:  $\pi_t^s$  CPI, weight sale flags

Constant	22.440*** (7.734)	18.541** (7.825)	2.616 (1.596)	2.665 (1.589)
Inflation $\pi_{t-1}$	-0.209 (0.129)	-0.194 (0.134)	-0.166 (0.142)	-0.154 (0.144)
Output gap $x_t$			0.053** (0.024)	
Output gap $x_{t-1}$				0.050** (0.024)
Unemp. rate $u_t$	-3.152*** (1.114)			
Unemp. rate $u_{t-1}$		-2.522** (1.125)		

# Empirical IRFs after a 1 sd Increase in Federal Funds Rate

Figure: Two VARs after a shock that increases the policy rate in UK. Each column is a VAR with different measure of inflation



# Conclusion

## Extensions

- Sales may be temporary but they are more frequent and attract more attention during downturns.
- This may understate the true inflation as prices reported by producers are not as volatile as what consumers pay.
- Moreover, recessions appear to be deeper when all agents and especially the CB responds to CPI instead of a sales-adjusted price index inflation.
- Placing more weight on sales items may revive the Phillips curve relationship